

# Color

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**Computer Graphics**  
**CMU 15-462/15-662**

**Why do we need to be able to talk precisely about color?**









**on screen**

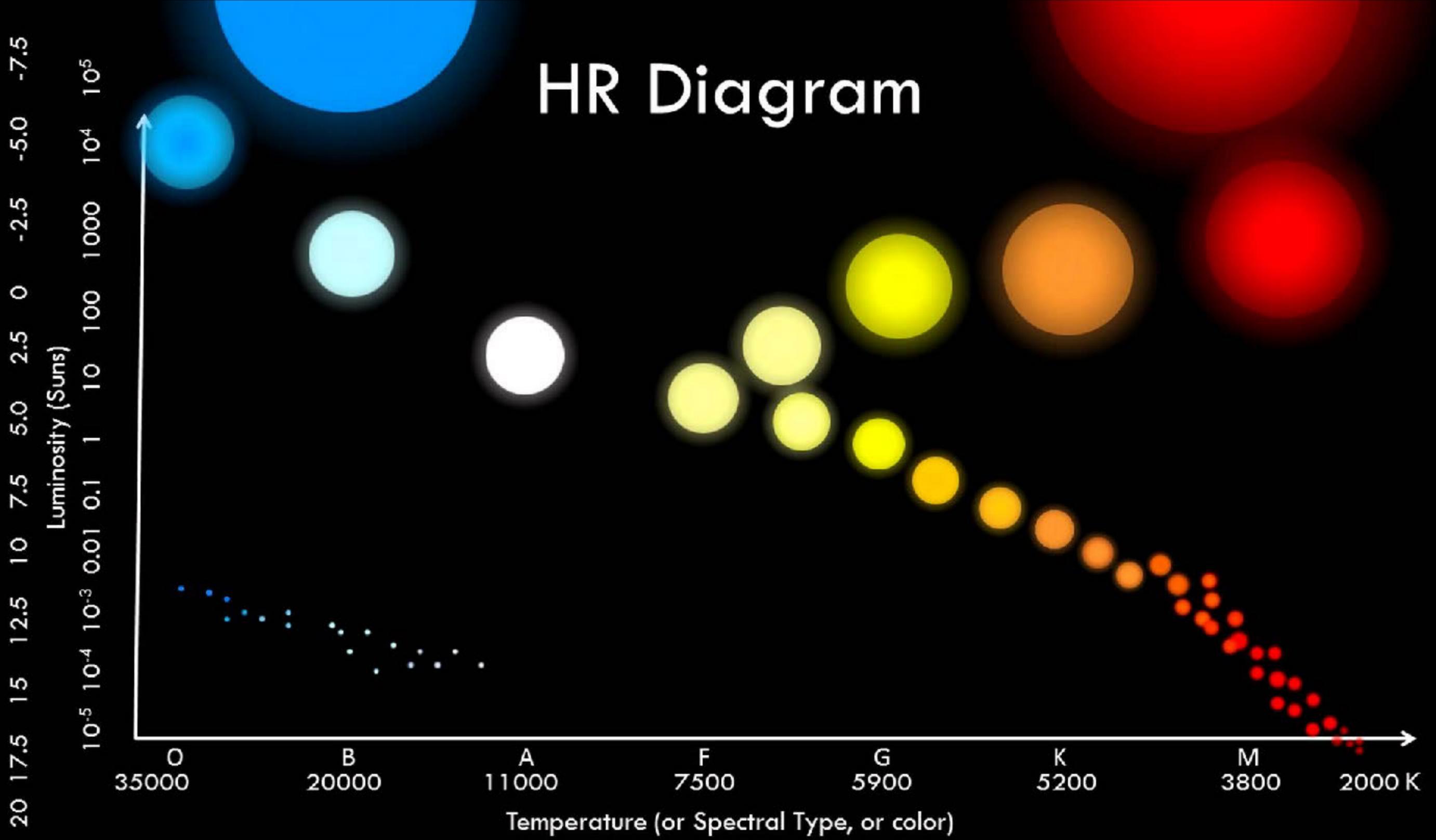


**printed**



**Zhangye Danxia Geological Park, China**

# HR Diagram



Hertzsprung-Russell diagram



Starry Night, Van Gogh



Cannon Beach, Oregon



**Vietnam**



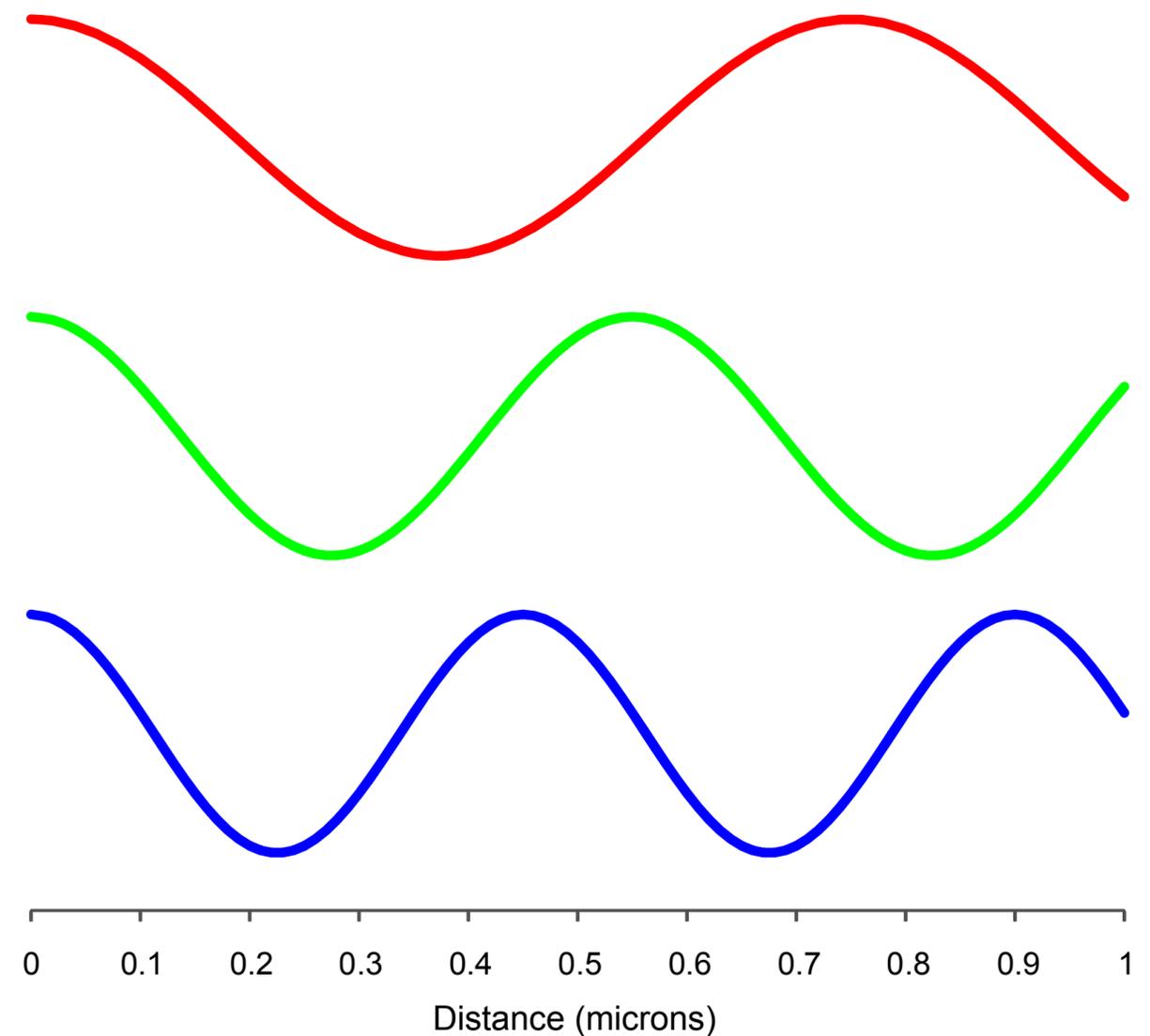
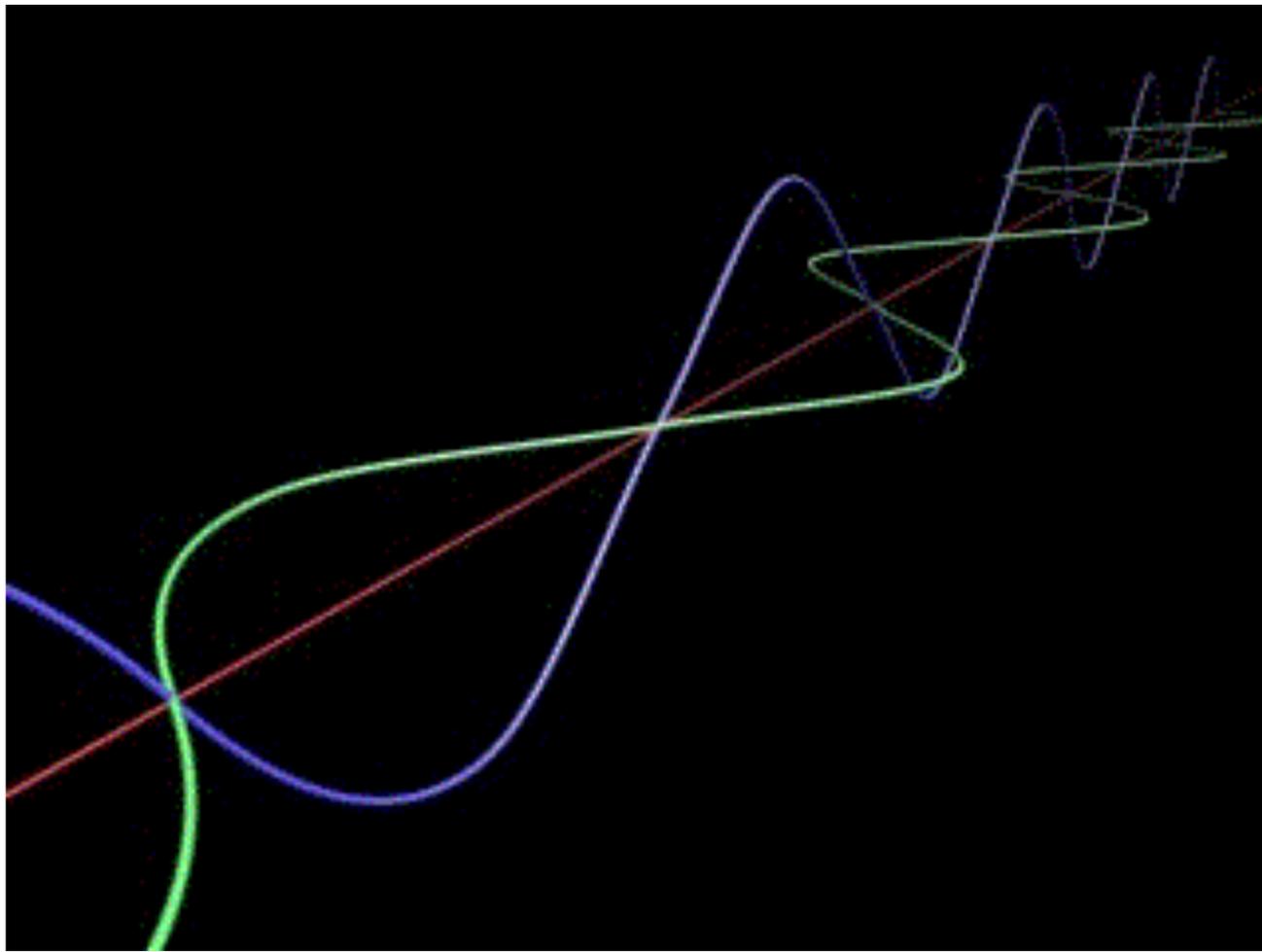


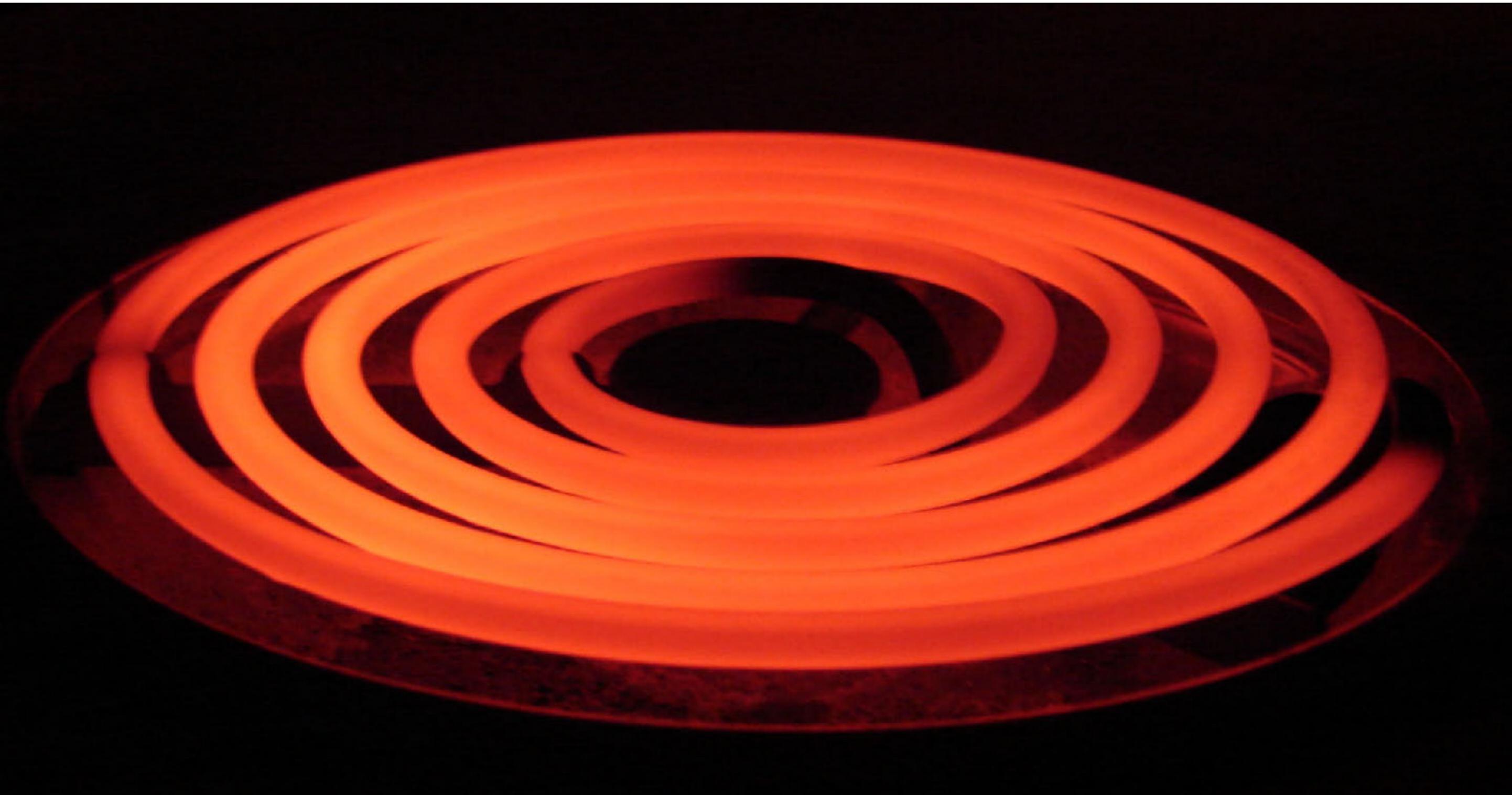
Sydney Harbor, Australia

# What is color?

# Light is EM Radiation; Color is Frequency

- Light is oscillating electric & magnetic field
- KEY IDEA: frequency determines color of light
- Q: What is the difference between *frequency* and *wavelength*?

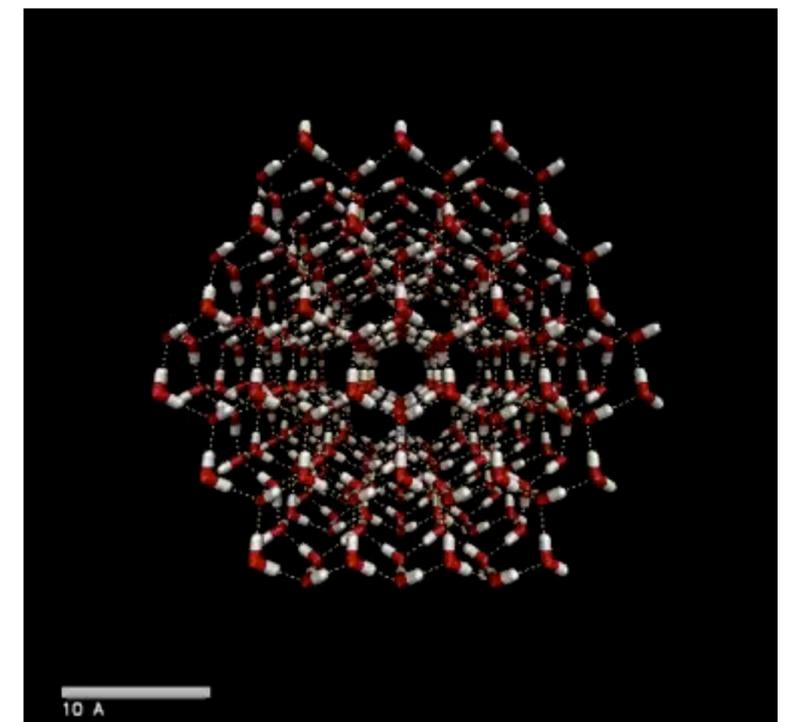
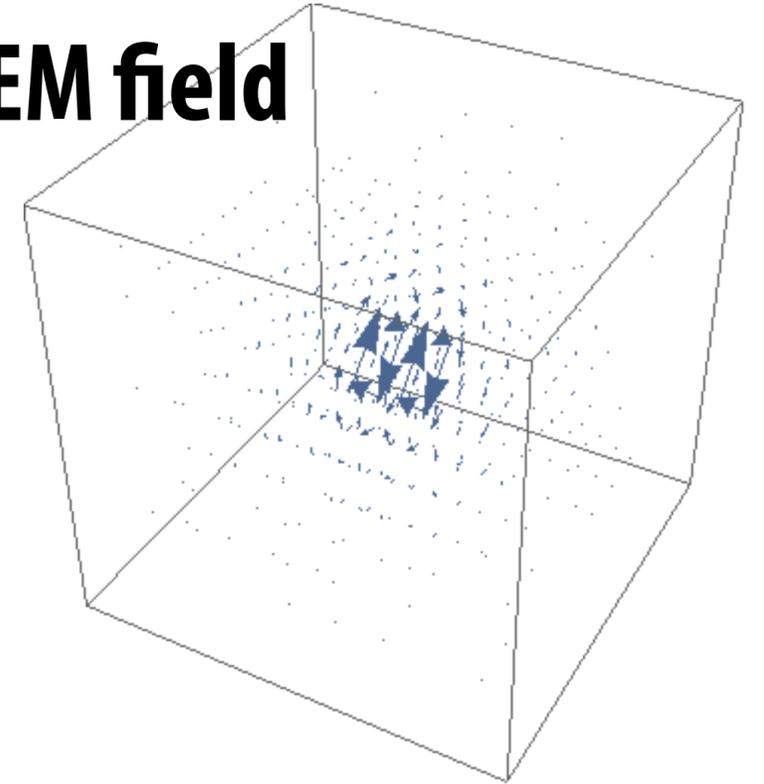




**Q: Why does your stove turn red when it heats up?**

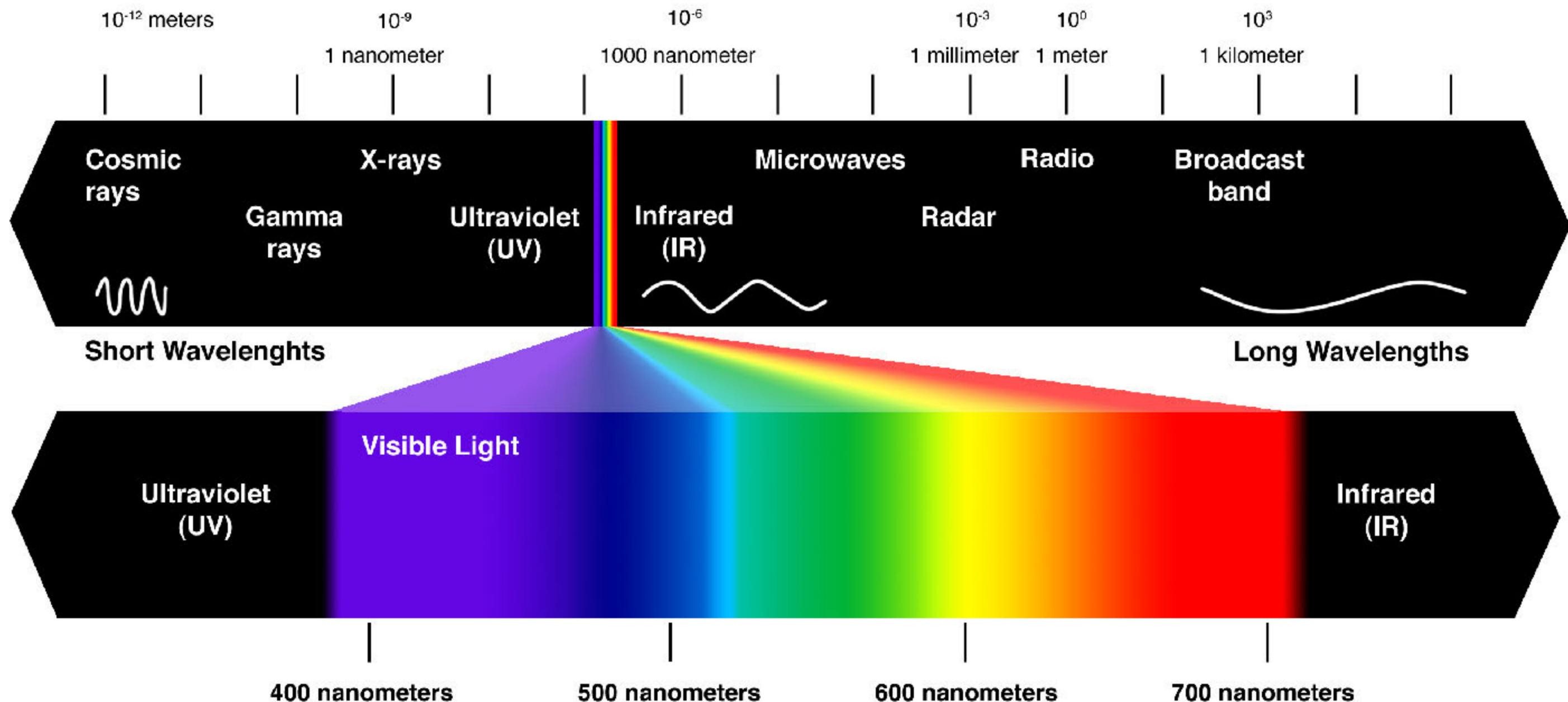
# Heat generates light

- One of *many* ways light is produced:
- Maxwell: motion of charged particles creates EM field
- Thermodynamics: ...particles jiggle around!
- Hence, anything moving generates light
- In other words:
  - *every* object around you is producing color!
  - frequency determined by temperature



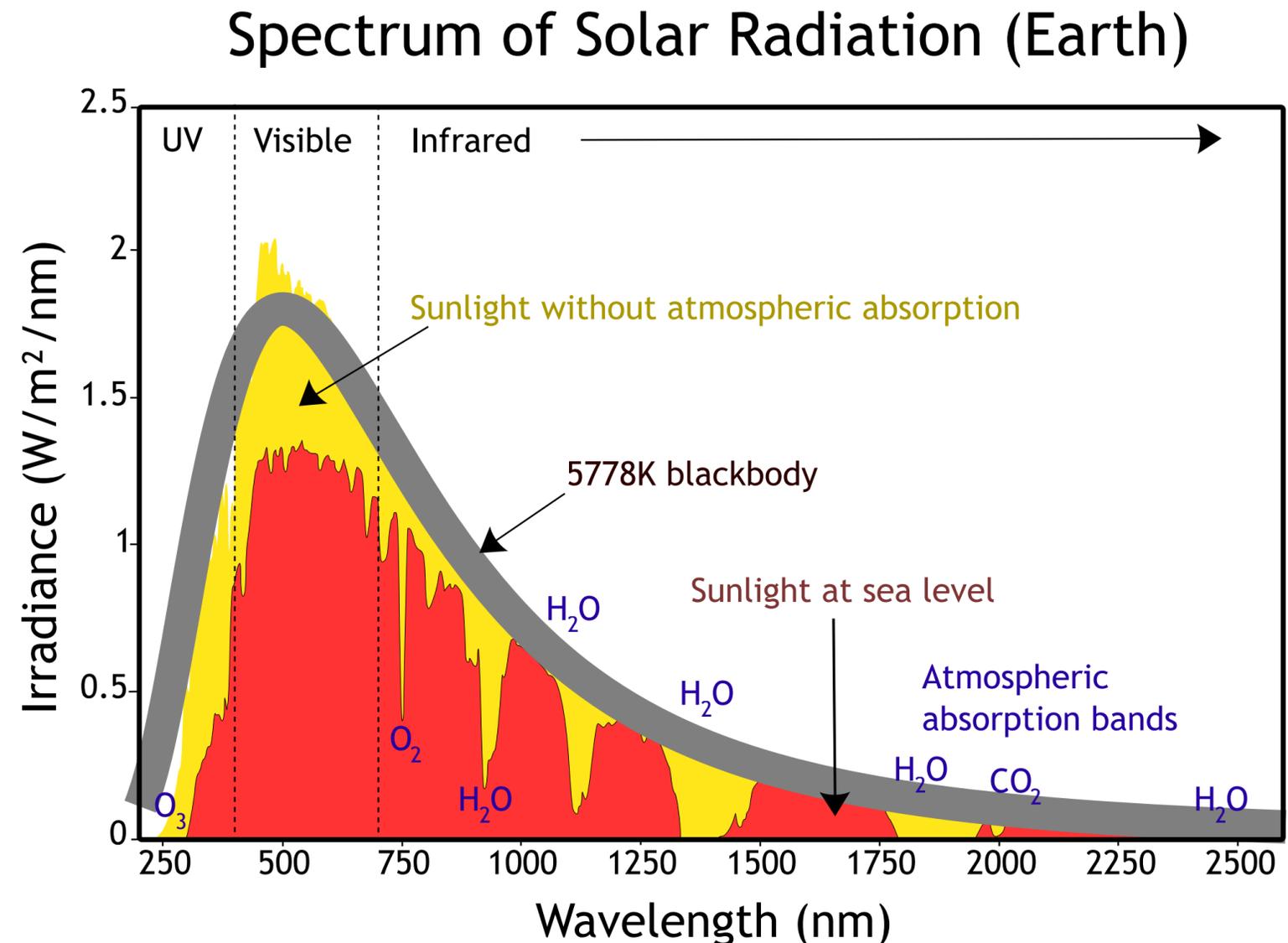
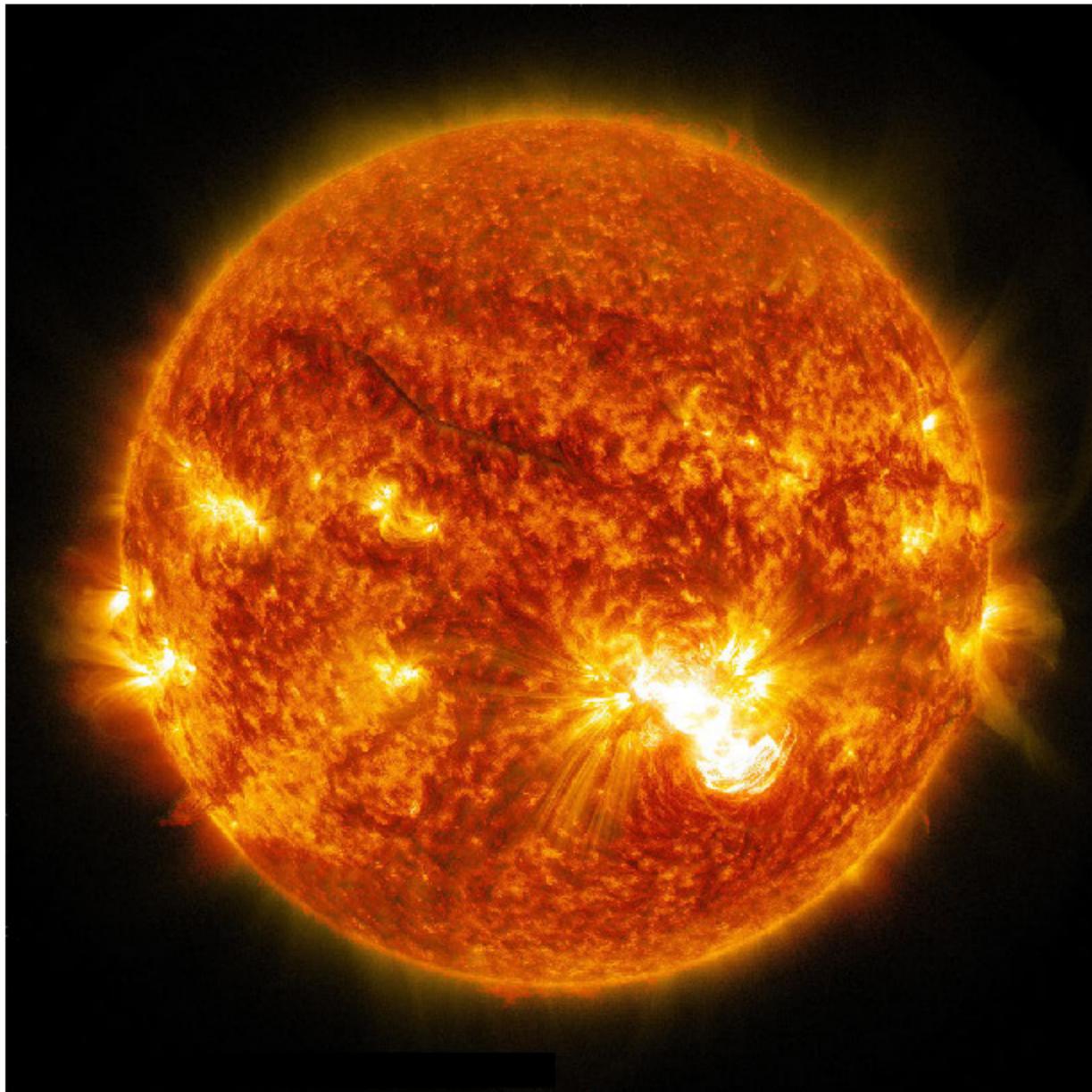
# Most light is not visible!

- Frequencies visible by human eyes are called “visible spectrum”
- These frequencies what we normally think of as “color”



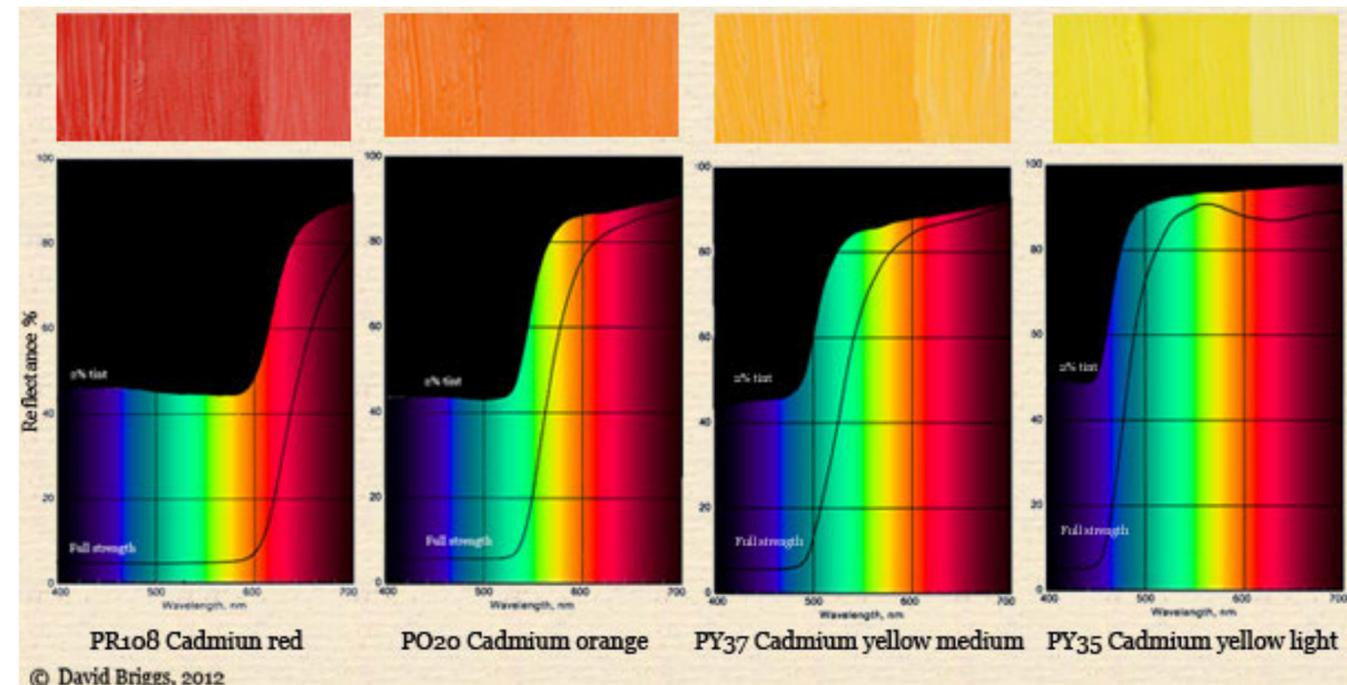
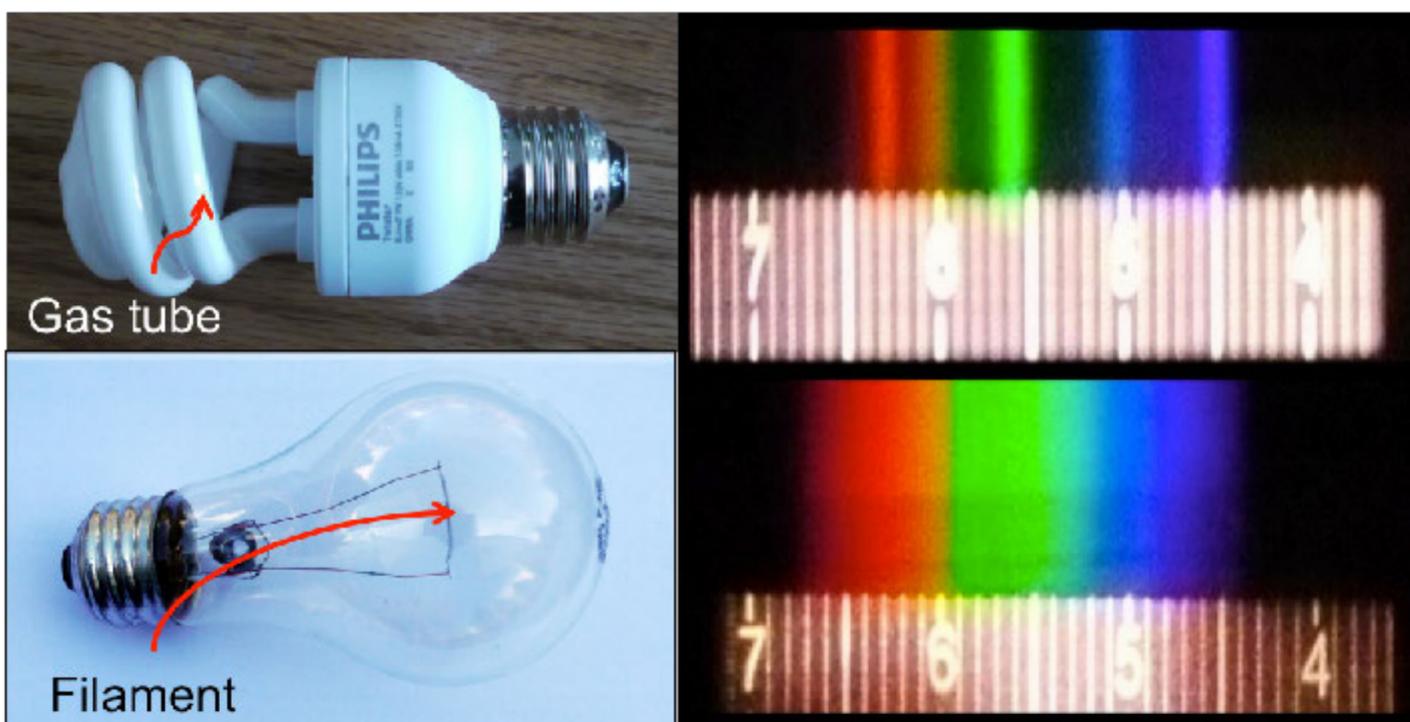
# Natural light is a mixture of frequencies

- “White” light is really a mixture of all (visible) frequencies
- E.g., the light from our sun



# Additive vs. Subtractive Models of Light

- Spectrum we just saw for the sun “*emission spectrum*”
  - How much light is *produced* (by heat, fusion, etc.)
  - Useful for, e.g., characterizing color of a lightbulb
- Another useful description: “*absorption spectrum*”
  - How much light is *absorbed* (e.g., turned *into* heat)
  - Useful for, e.g., characterizing color of paint, ink, etc.



# Emission Spectrum

Describes light intensity as a function of frequency

Below: spectrum of various common light sources:

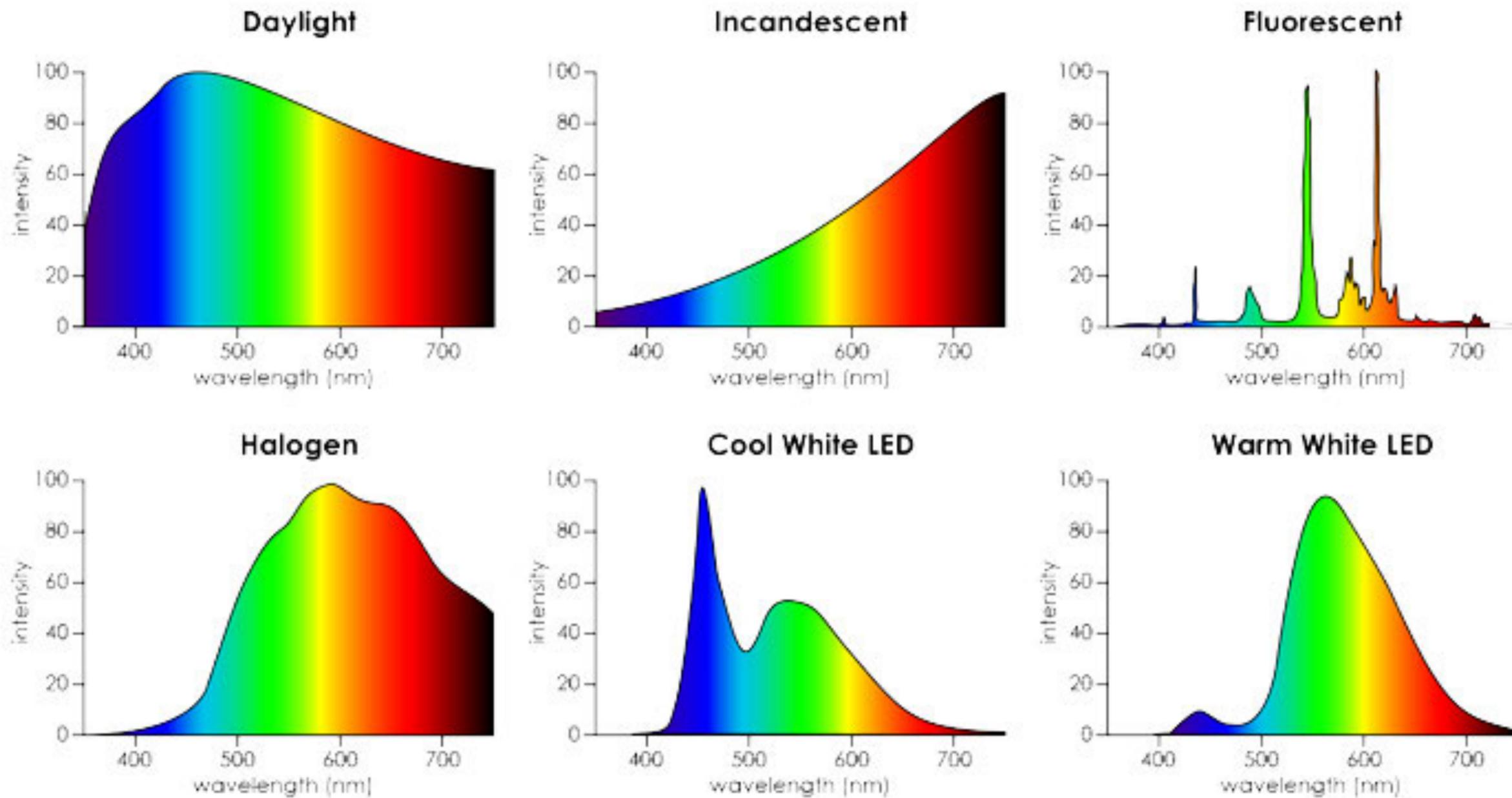
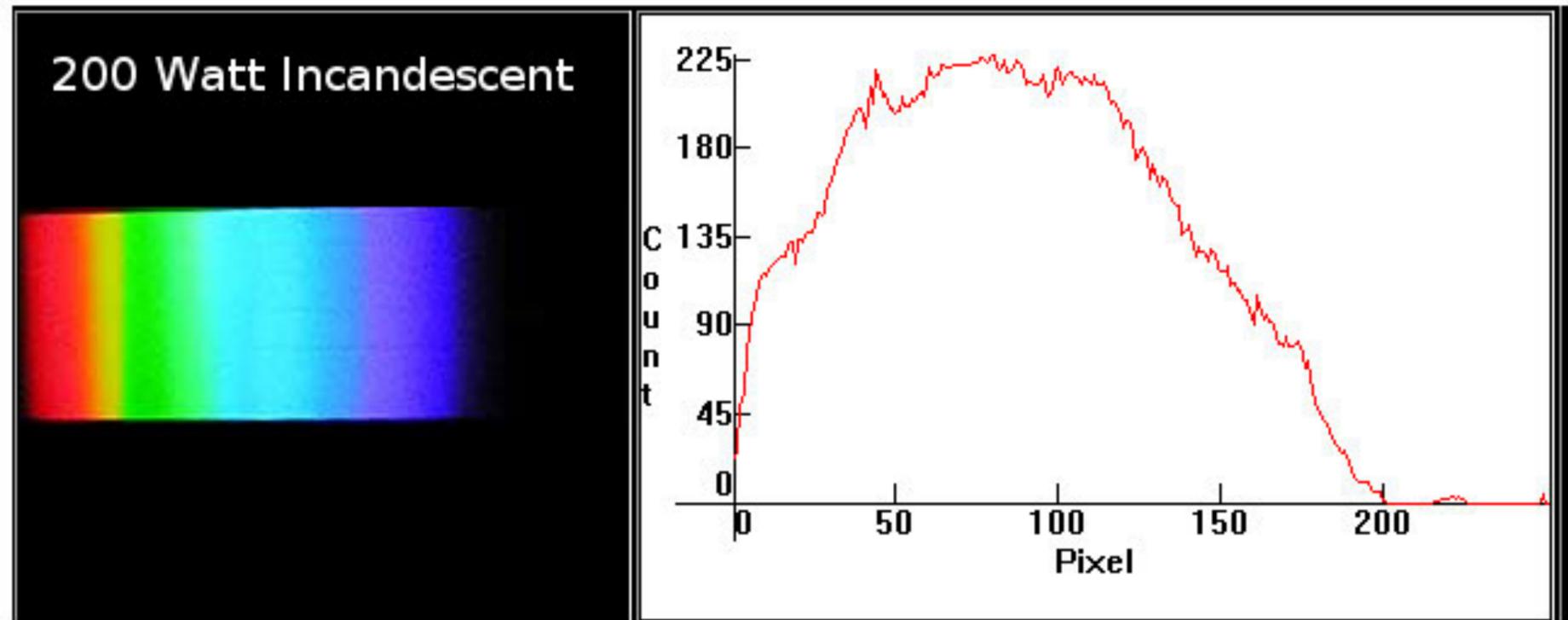


Figure credit:

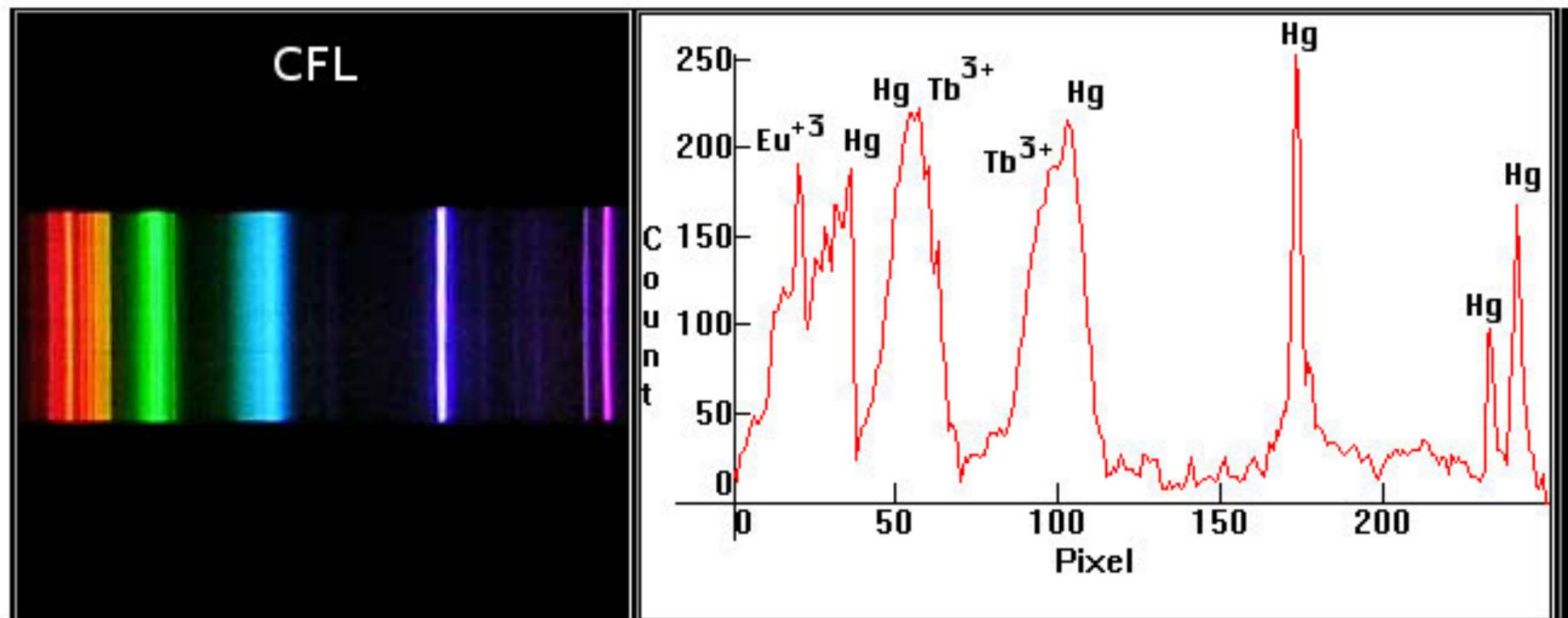
# Emission Spectrum—Example

- Why so many different kinds of lightbulbs on the market?
- “Quality” of light:

**Incandescent:**  
+more sun-like  
-power-hungry

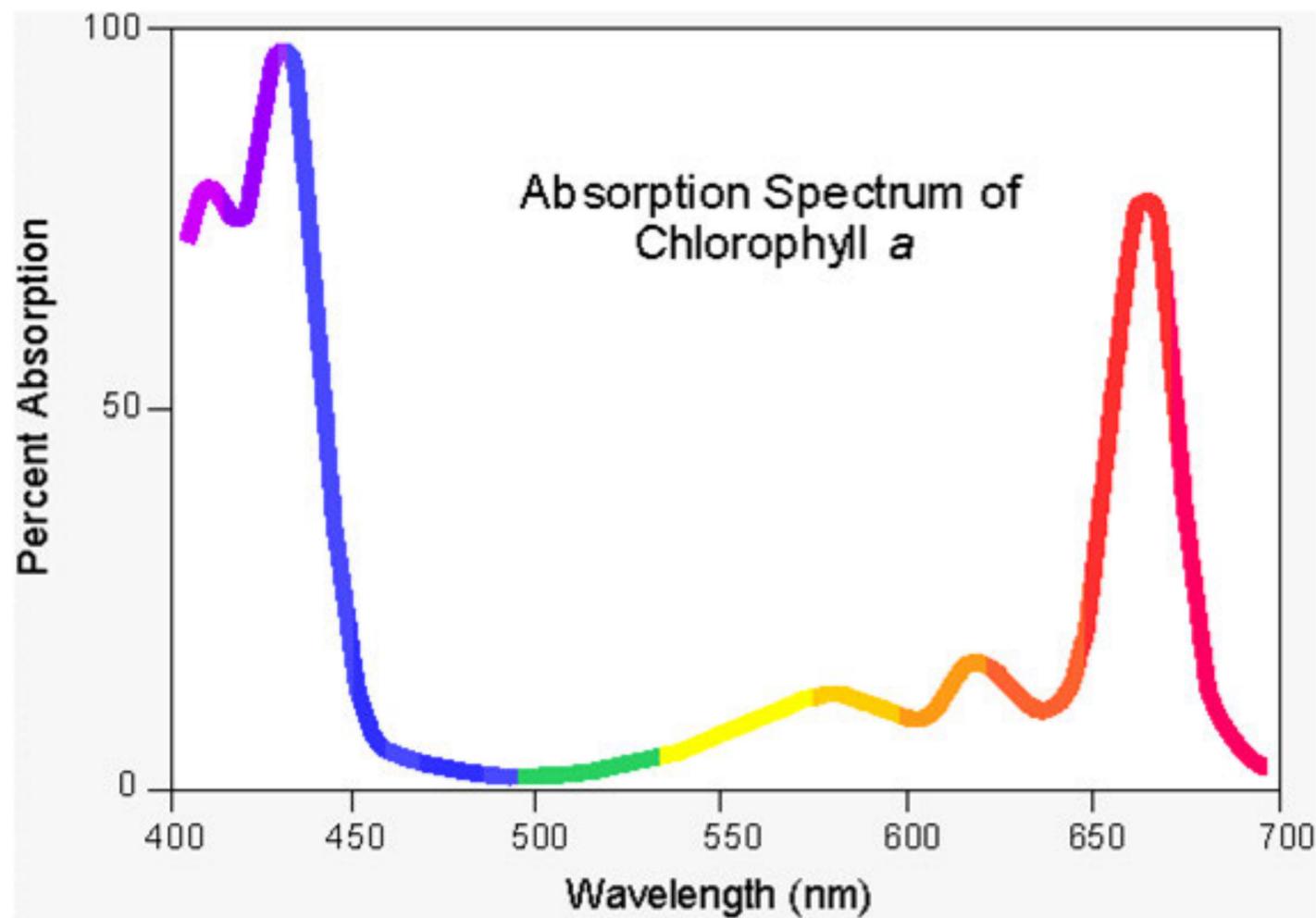


**CFL:**  
-“choppy” spectrum  
+power efficient



# Absorption Spectrum

- Emission spectrum is *intensity* as a function of frequency
- Absorption spectrum is *fraction absorbed* as function of frequency



**Q: What color is an object with this absorption spectrum?**

**This is the fundamental description of color:  
*intensity or absorption as a function of frequency***



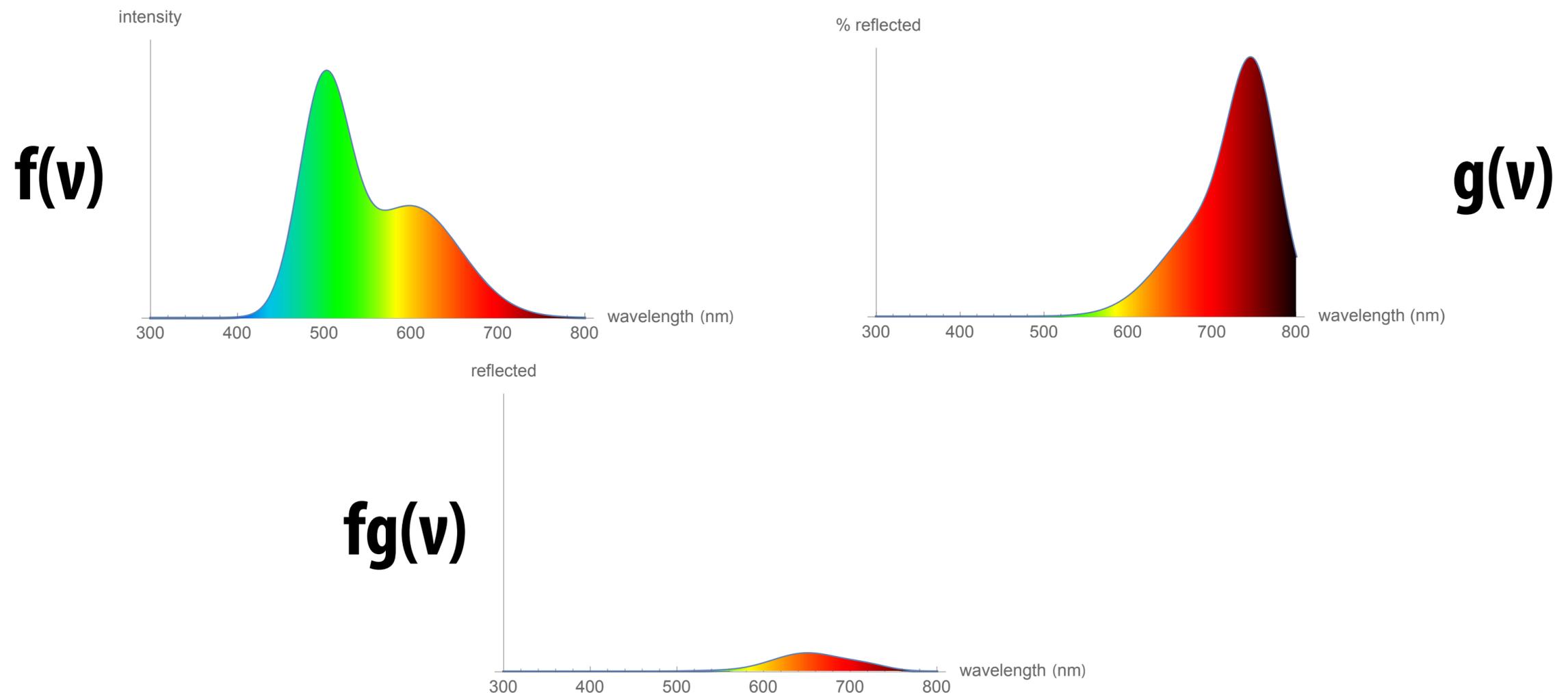
***Everything else is merely a convenient approximation!***

**If you remember to use spectral description as a starting point, the issues surrounding color theory/ practice will make a *lot* more sense!**

**If on the other hand you always think of color in terms of approximate digital encodings (RGB, CMYK) etc., there are certain phenomena you simply cannot explain/understand!**

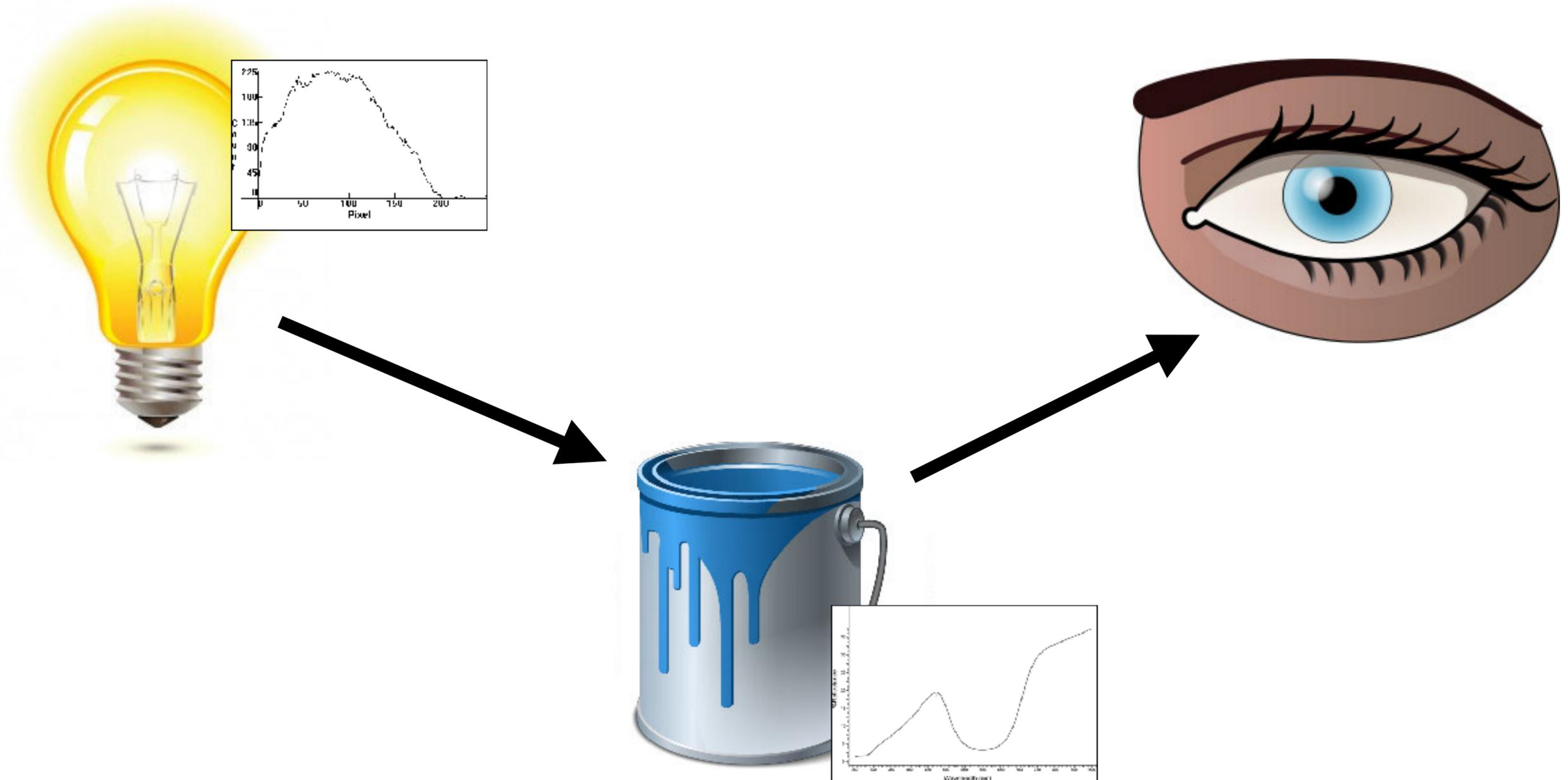
# Reflection is emission times absorption

- Toy model for what happens when light gets reflected
  - $\nu$ —frequency (Greek “nu”)
  - Light source has emission spectrum  $f(\nu)$
  - Surface has reflection spectrum  $g(\nu)$
  - Resulting intensity is the *product*  $f(\nu)g(\nu)$



# Color reproduction is hard!

- Color clearly starts to get complicated as we start combining emission and absorption/reflection (real-world challenge!)



**(What color ink should we use to get the desired appearance?)**

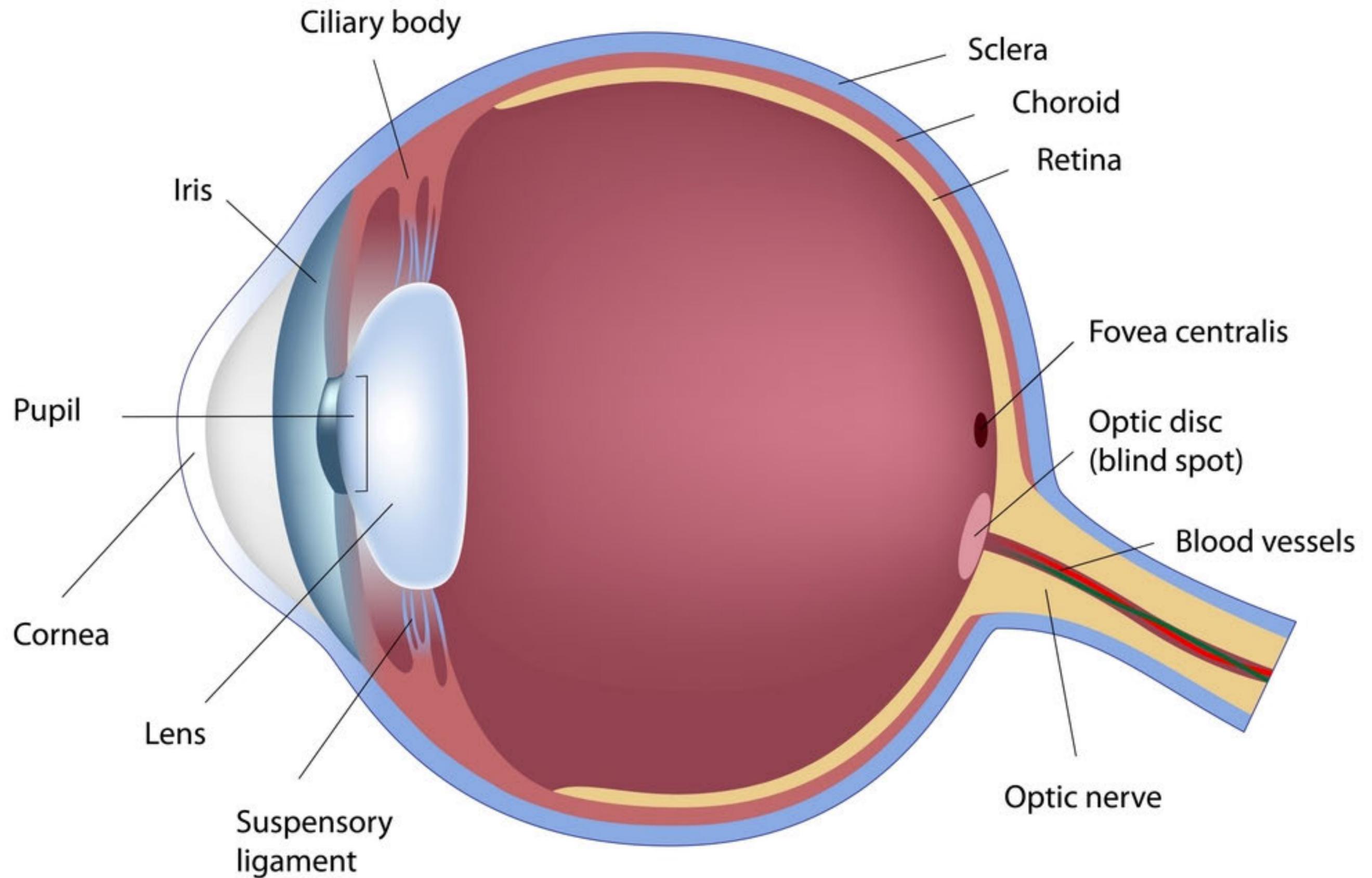
# ...And what about perception?

**Q: What color is this dress?**

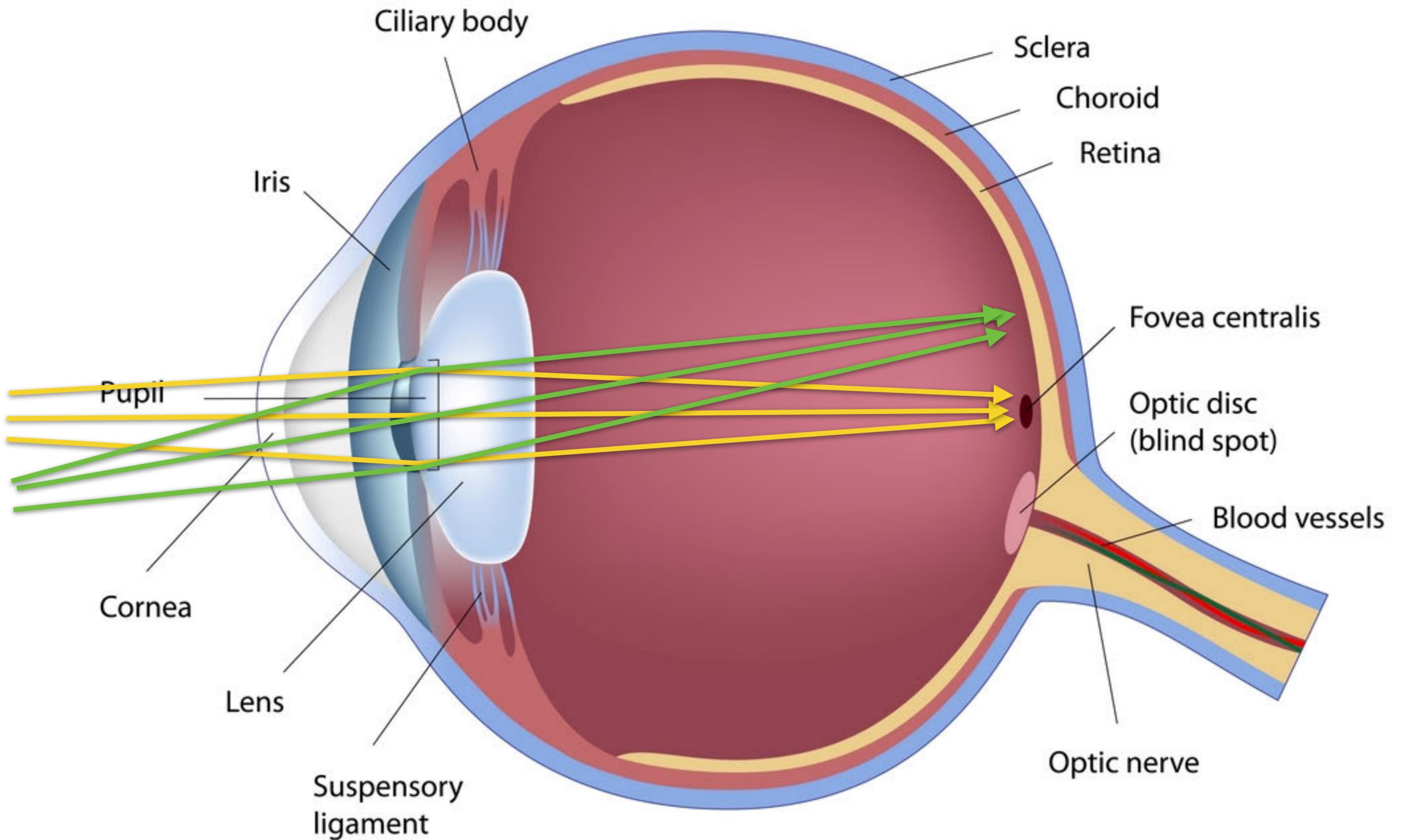


**How does electromagnetic radiation (with a given power distribution) end up being perceived by a human as a certain color?**

# The eye



# The eye (optics)



# Photosensor response (eye, camera, ...)

## ■ Photosensor input: light

- Electromagnetic power distribution over wavelengths:  $\Phi(\lambda)$

## ■ Photosensor output: a “response” ... a number

- e.g., encoded in electrical signal

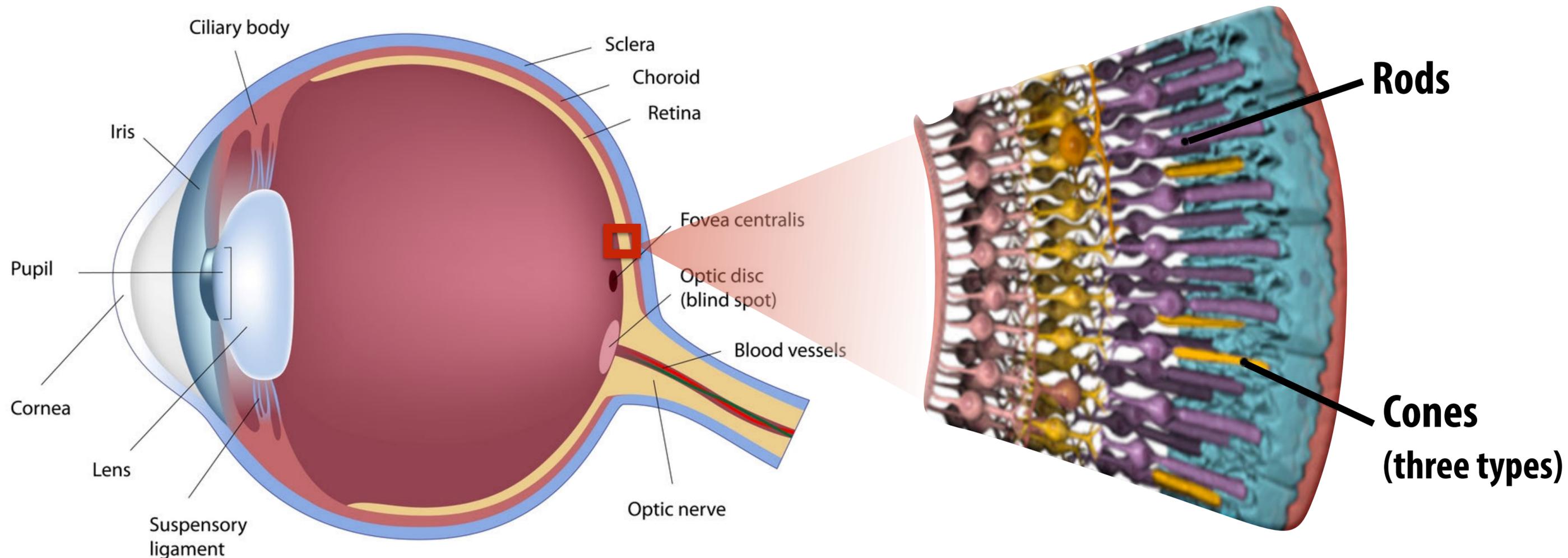
## ■ Spectral response function: $f(\lambda)$

- Sensitivity of sensor to light of a given wavelength
- Greater  $f(\lambda)$  corresponds to more a efficient sensor (when  $f(\lambda)$  is large, a small amount of light at wavelength  $\lambda$  will trigger a large sensor response)

## ■ Total response of photosensor:

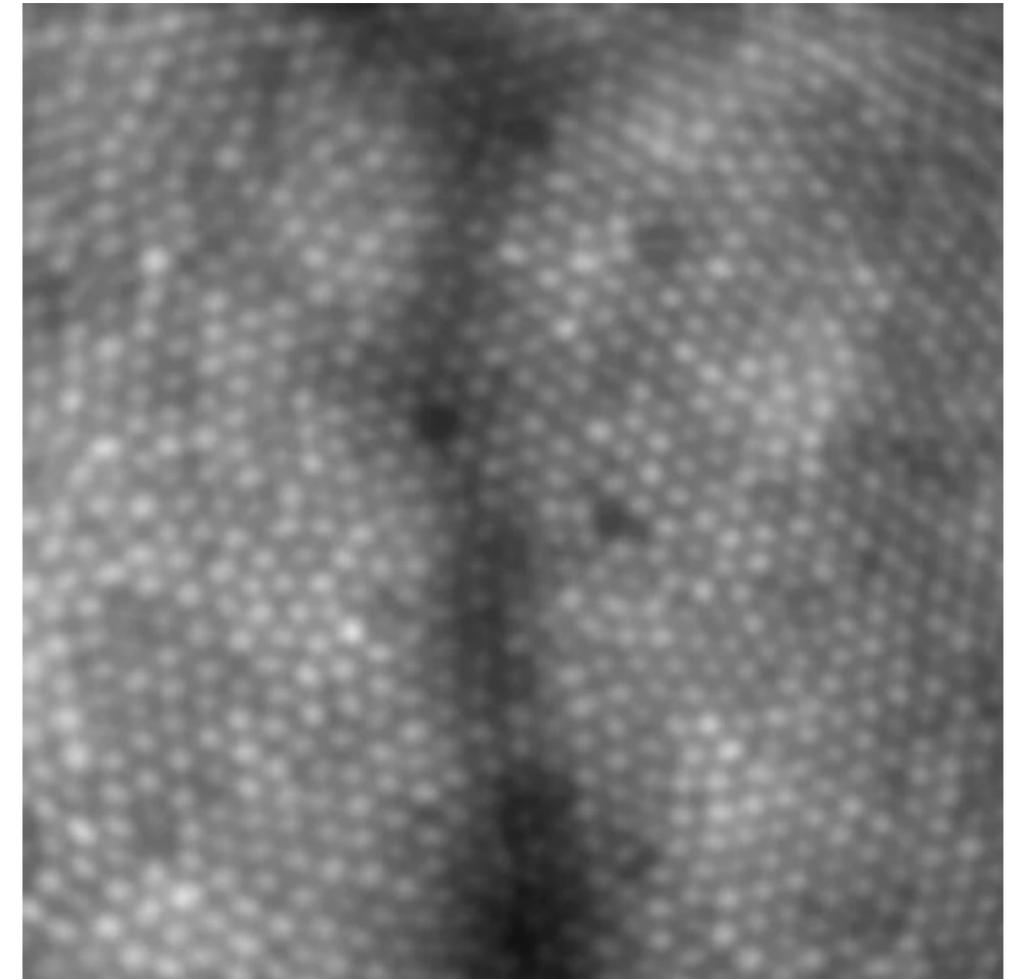
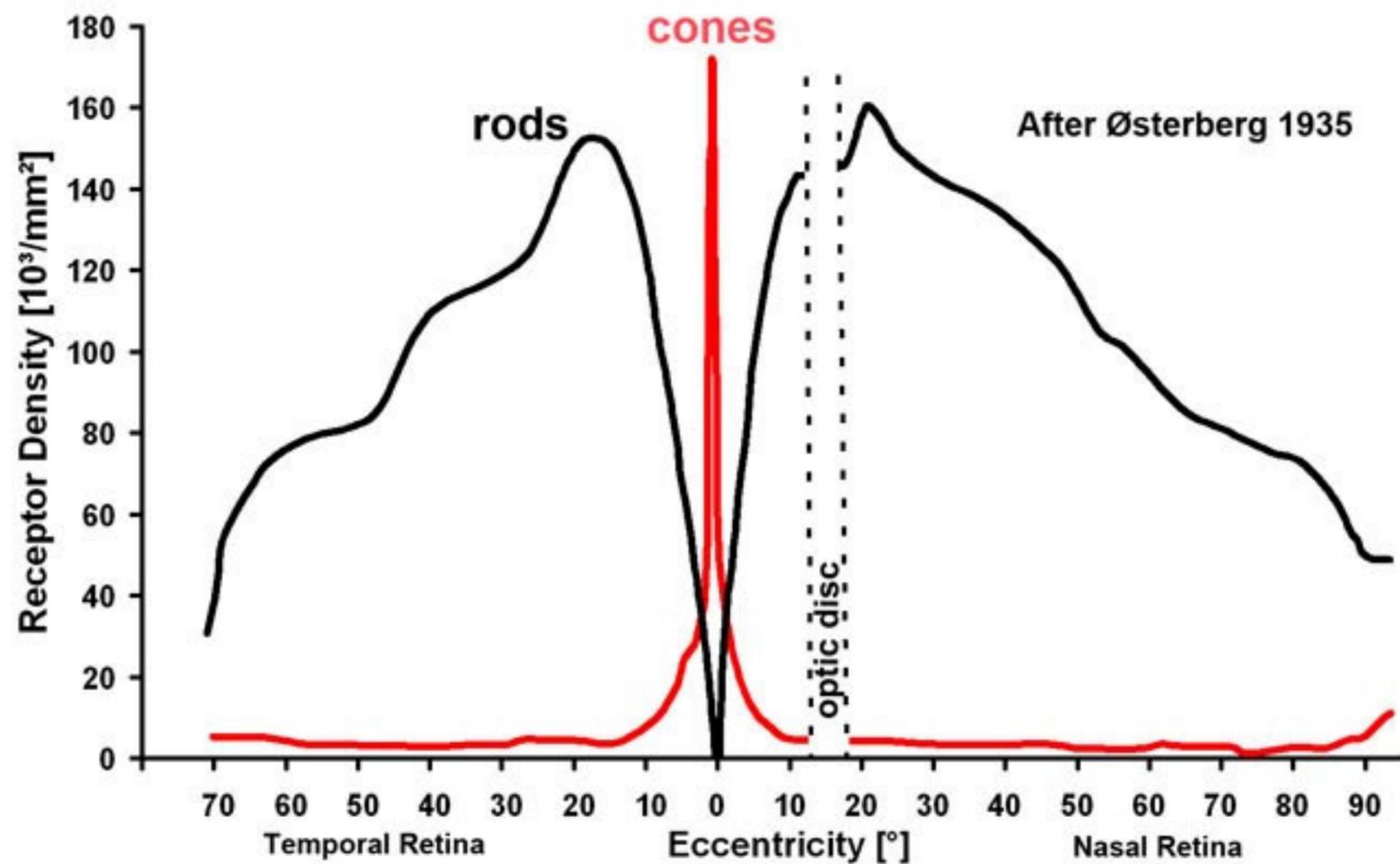
$$R = \int_{\lambda} \Phi(\lambda) f(\lambda) d\lambda$$

# The eye's photoreceptor cells: rods & cones



- **Rods are primary receptors under dark viewing conditions (scotopic conditions)**
  - Approx. 120 million rods in human eye
- **Cones are primary receptors under high-light viewing conditions (photopic conditions, e.g., daylight)**
  - Approx. 6-7 million cones in the human eye
  - Each of the three types of cone feature a different spectral response. This will be critical to color vision (much more on this in the coming slides)

# Density of rods and cones in the retina



[Roorda 1999]

- Highest density of cones is in fovea  
(best color vision at center of where human is looking)
- Note “blind spot” due to optic nerve

# ACTIVITY: Rods vs. Cones

- Need a brave volunteer from the audience!
  - Will hold up colored marker in peripheral vision
  - All you have to do is tell us what color it is (easy!)



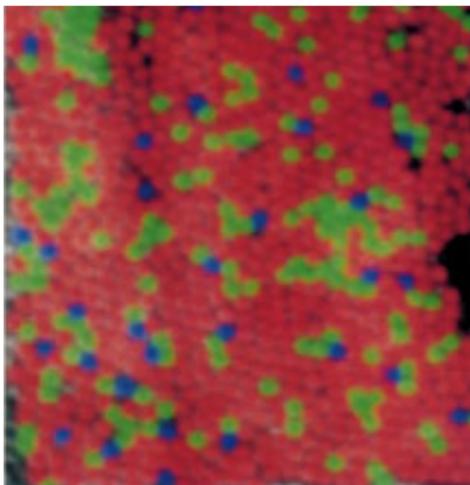
# Spectral response of cones

Three types of cones: S, M, and L cones (corresponding to peak response at short, medium, and long wavelengths)

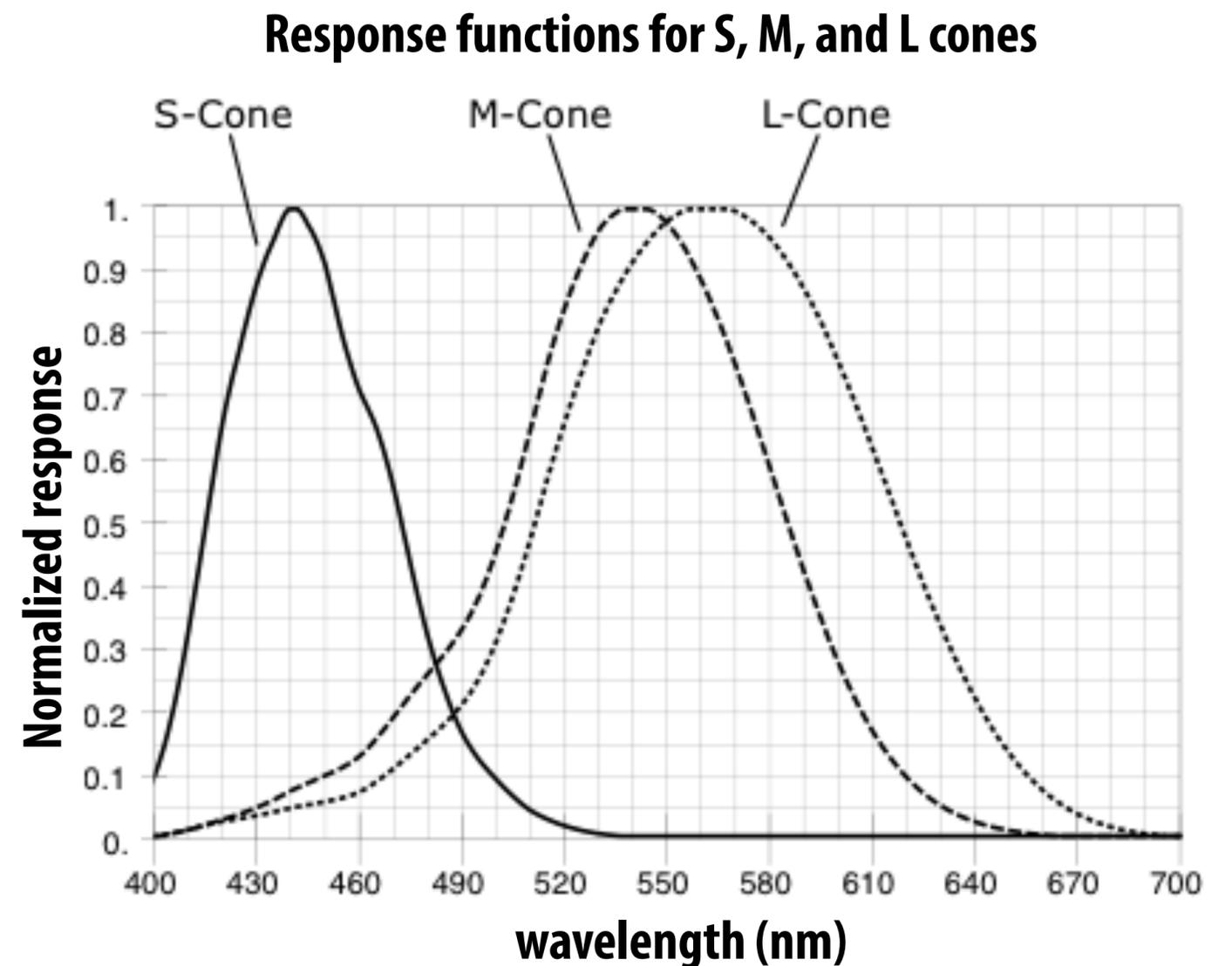
$$S = \int_{\lambda} \Phi(\lambda) S(\lambda) d\lambda$$

$$M = \int_{\lambda} \Phi(\lambda) M(\lambda) d\lambda$$

$$L = \int_{\lambda} \Phi(\lambda) L(\lambda) d\lambda$$



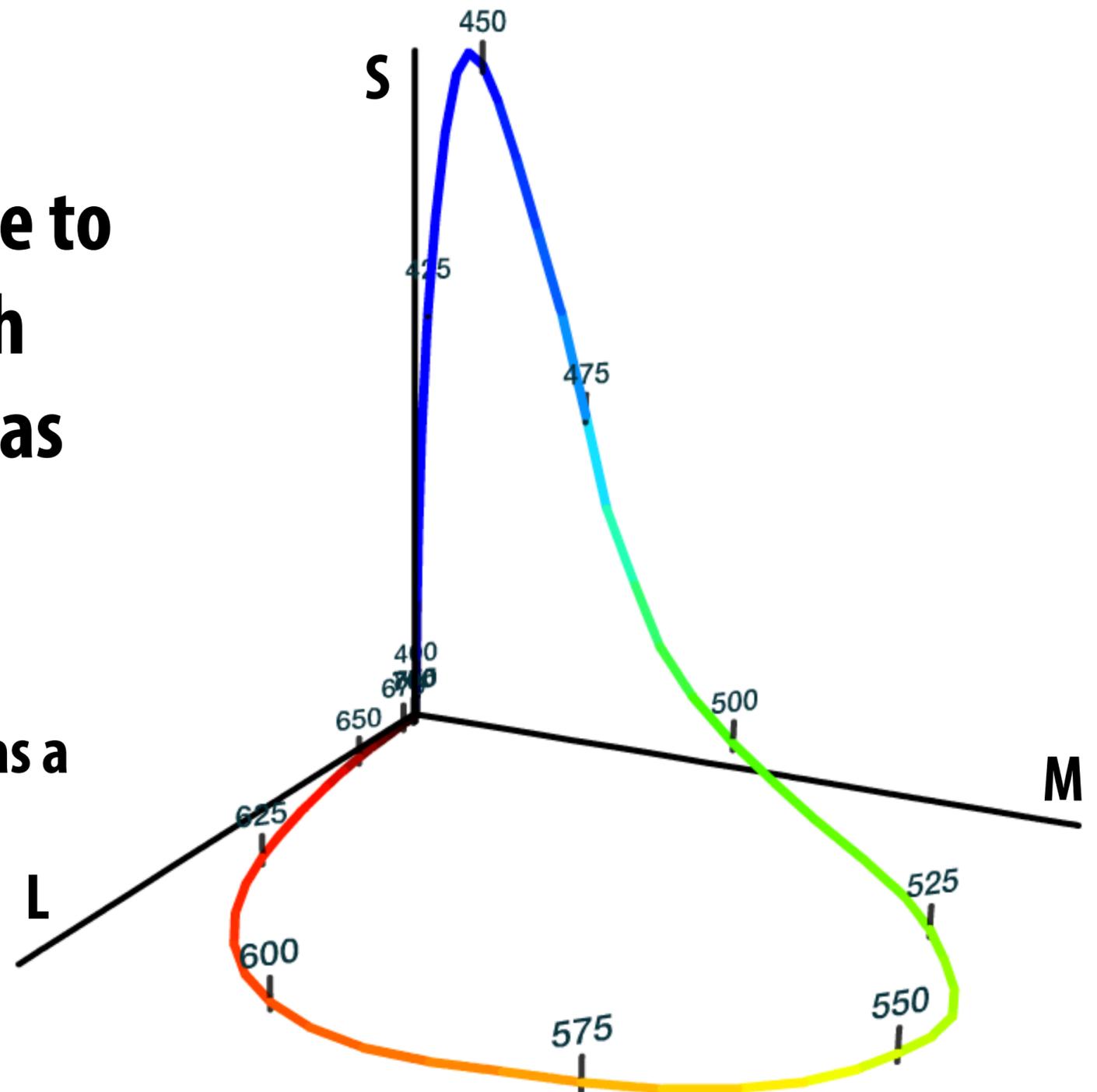
Uneven distribution of cone types in eye  
~64% of cones are L cones, ~ 32% M cones



# Response of S,M,L cones to monochromatic light

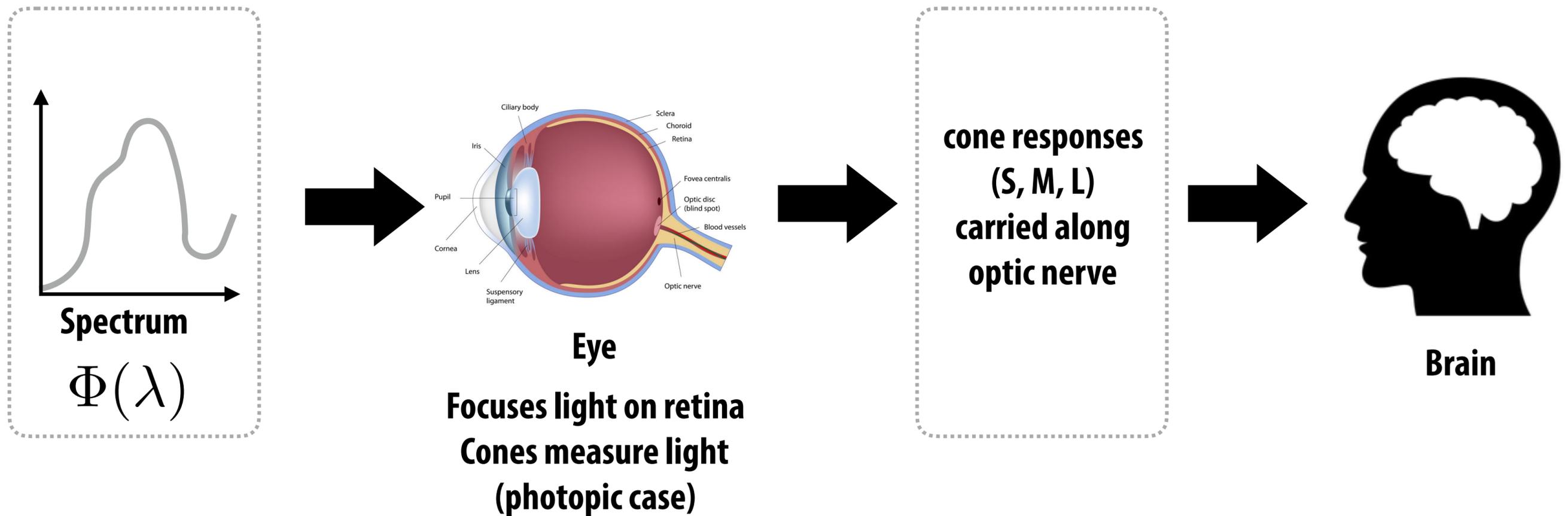
Figure visualizes cone's response to monochromatic light (light with energy in a single wavelength) as points in 3D space

(plots value of S, M, L response functions as a point in 3D space)



# The human visual system

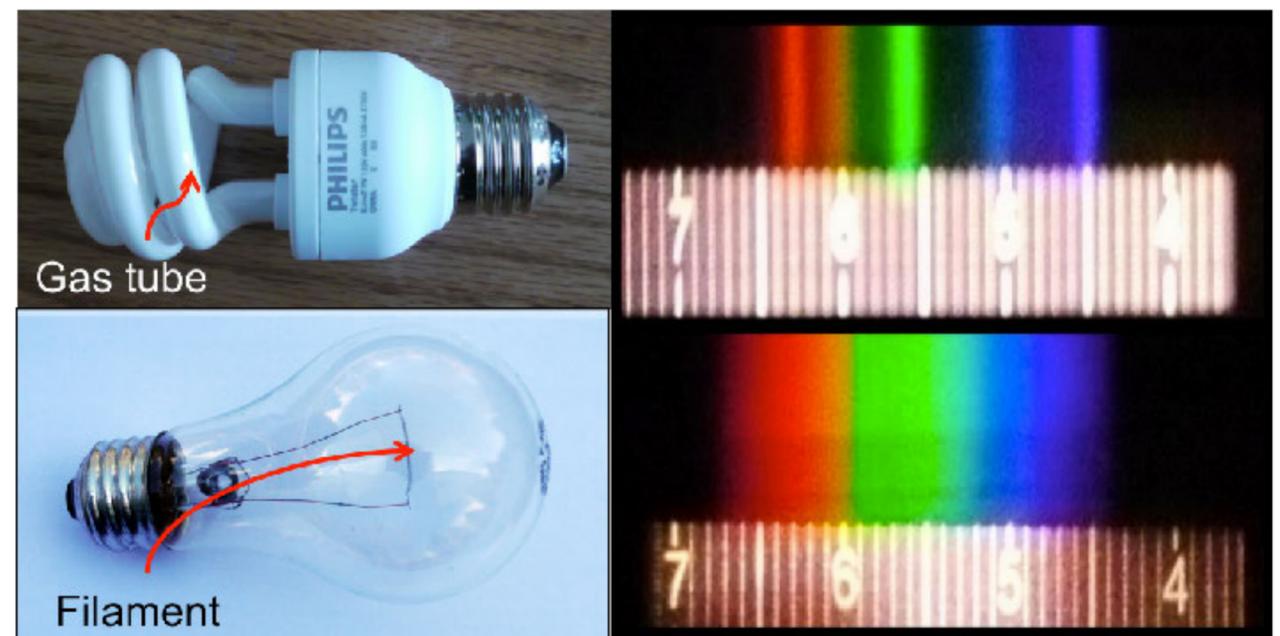
- Human eye does not directly measure the spectrum of incoming light
  - i.e., the brain does not receive “a spectrum” from the eye
- The eye measures three response values = (S, M, L). The result of integrating the incoming spectrum against response functions of S, M, L-cones



**Q: Is it possible for two functions  
to integrate to the same value?**

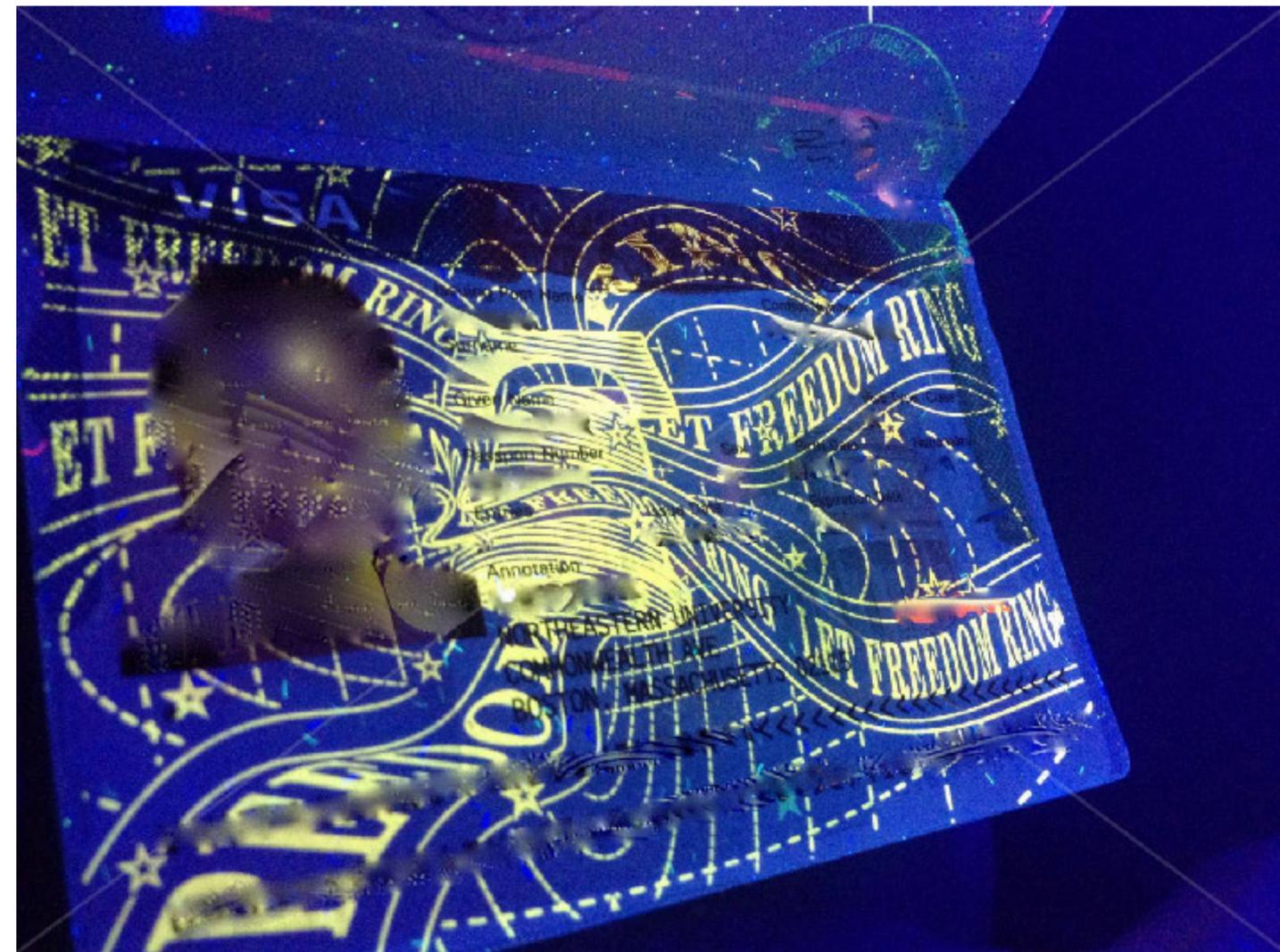
# Metamers

- **Metamers = two different spectra that integrate to the same (S,M,L) response!**
- **The fact that metameters exist is critical to color reproduction: we don't have to reproduce the exact same spectrum that was present in a real world scene in order to reproduce the *perceived* color on a monitor (or piece of paper, or paint on a wall)**
- **...On the other hand, combination of light & paint could still cause trouble—different objects appearing “wrong” under different lighting conditions.**



# Example: Counterfeit Detection

- Many countries print currency, passports, etc., with special inks that yield different appearance under UV light:

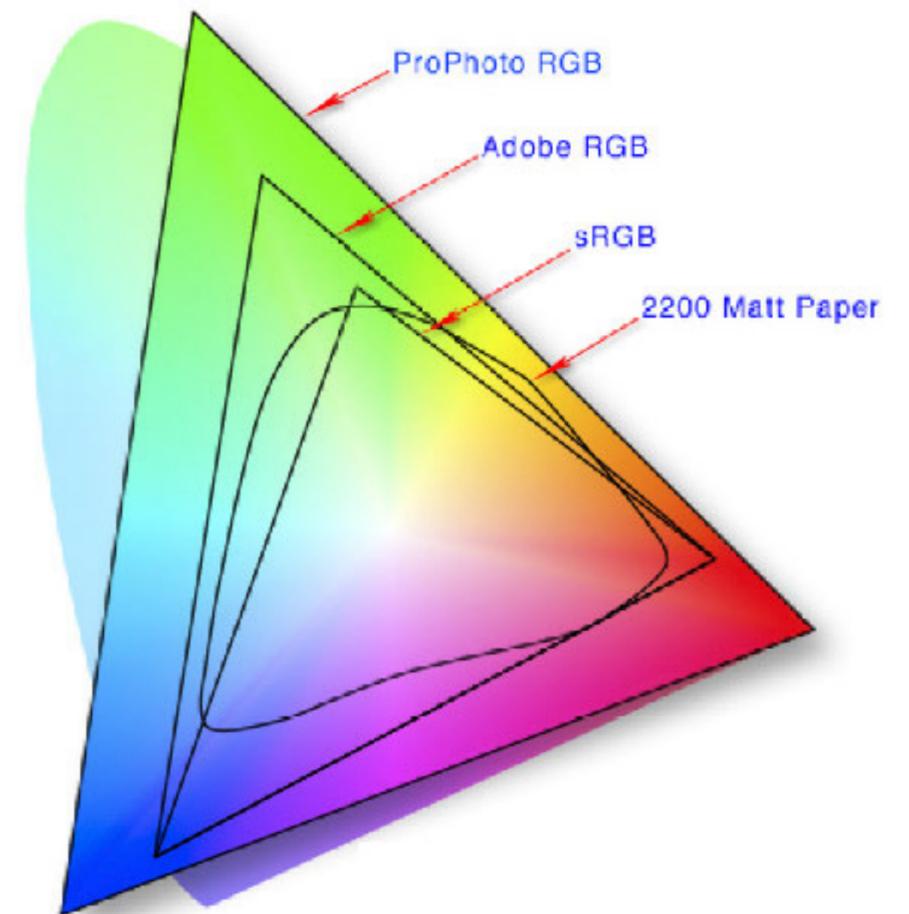


**Ok, so color can get pretty complicated!**

**How do we encode it in a simple(r) way?**

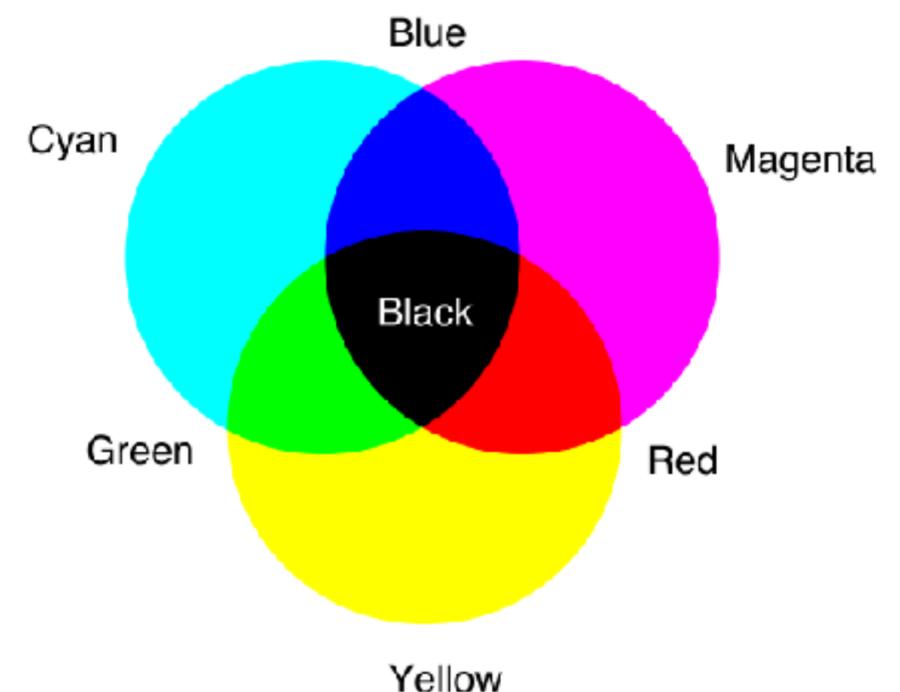
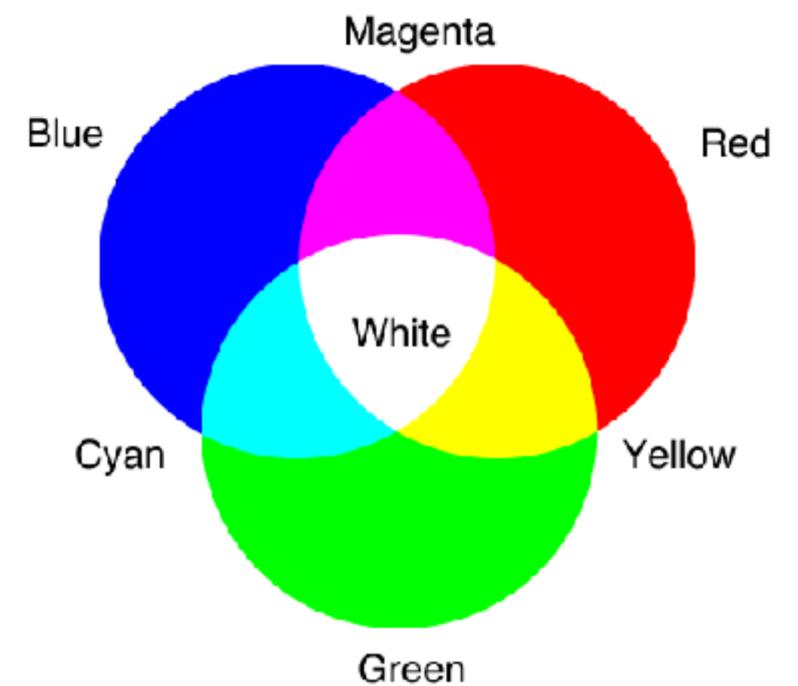
# Color Spaces and Color Models

- Many ways to specify a color
  - storage
  - convenience
- In general, specify a color from some *color space* using a *color model*
- *Color space* is like artist's palette: full range of colors we can choose from
- *Color model* is the way a particular color in a color space is specified:
  - artist's palette: "yellow ochre"
  - RGB color model: 204, 119, 34



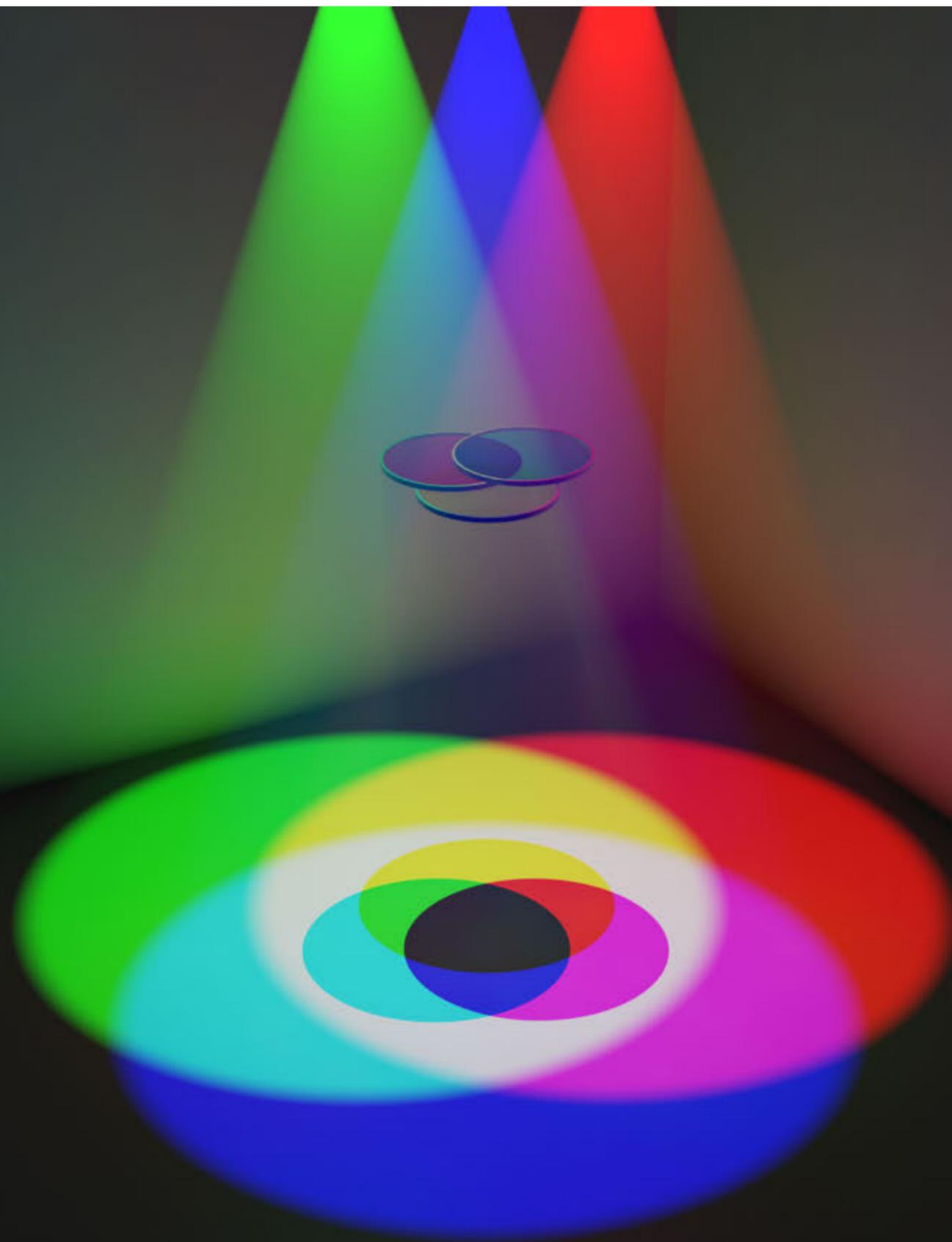
# Additive vs. Subtractive Color Models

- Just like we had emission & absorption spectra, we have *additive* and *subtractive*\* color models
- Additive
  - Used for, e.g., combining colored lights
  - Prototypical example: RGB
- Subtractive
  - Used for, e.g., combining paint colors
  - Prototypical example: CMYK



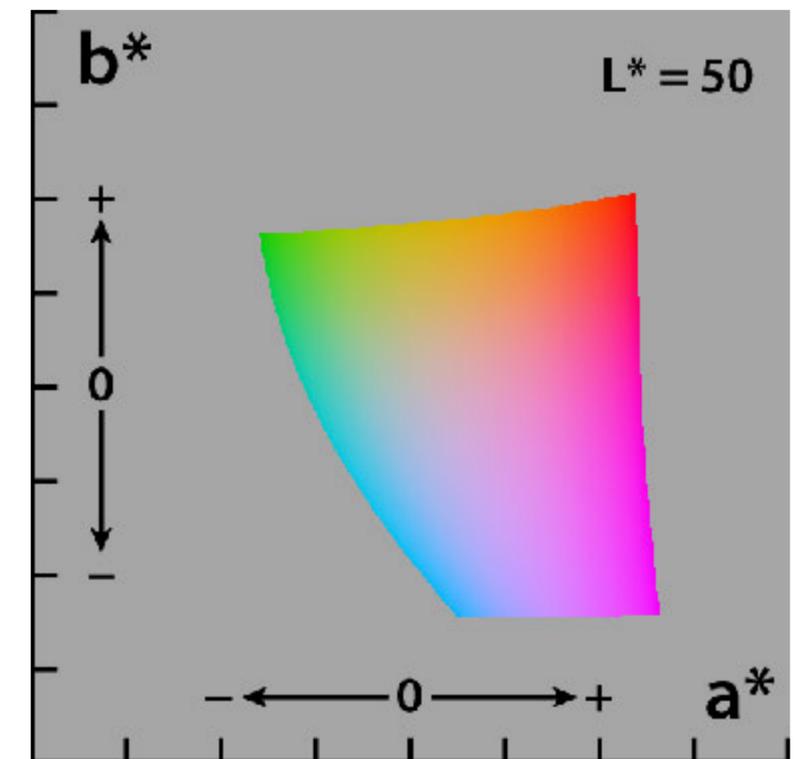
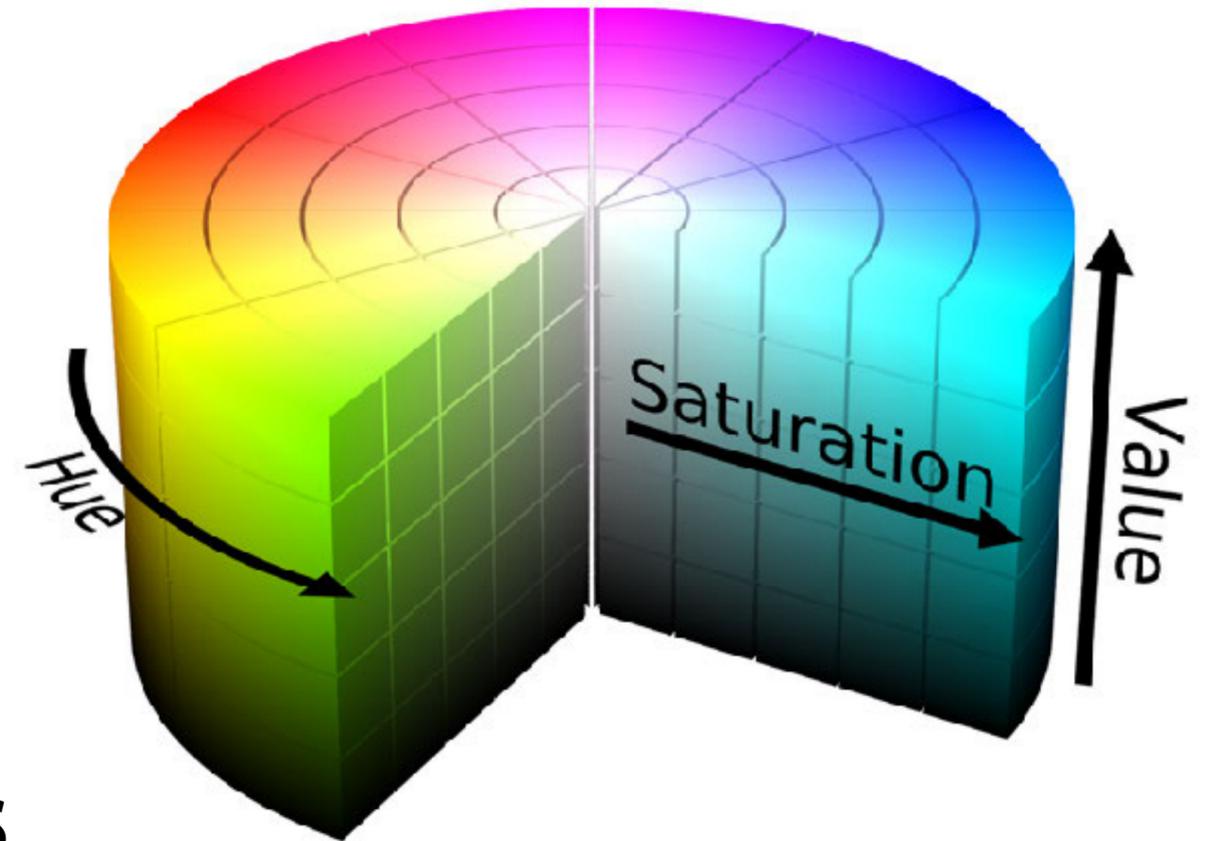
\*A better name than subtractive might be *multiplicative*, since we *multiply* to get the final color!

# Let's shed some light on this picture...



# Other Common Color Models

- **HSV**
  - hue, saturation, value
  - more intuitive than RGB/CMYK
- **SML—physiological model**
  - corresponds to stimulus of cones
  - not practical for most color work
- **XYZ—preceptually-driven model**
  - Y captures *luminance* (intensity)
  - X,Z capture *chromaticity* (color)
  - related to, but different from, SML
- **Lab—“perceptually uniform” modification of XYZ**



# Practical Encoding of Color Values

- How do colors actually get encoded digitally?
- One common encoding (e.g., HTML): *8bpc hexadecimal values\**:

**# 1B1F8A**

- What does this string mean? Common encoding of RGB.
- Want to store 8-bits per channel (red, green, blue), corresponding to 256 possible values
- Rather than use digits 0-9, use 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, **A, B, C, D, E, F**
- Single character now encodes 16 values, two characters encode  $16 * 16 = 256$  values
- Q: Roughly what color is # 1B1F8A?



\*Upper vs. lowercase letters? Makes absolutely *no* difference!

# Other Ways of Specifying Color?

- Other color specifications not based on continuous color space
- E.g., Pantone Matching System
  - industry standard (proprietary)
  - 1,114 colors
  - Combination of 13 base pigments
- And not to forget...



# Why use different color models?

- **Convenience**

- **Is it easy for a user to choose the color they want?**

- **Efficiency of encoding**

- **E.g., use more of numerical range for perceptually significant colors**
- **Do color images *compress* well?**

# Example: Y'CbCr color model

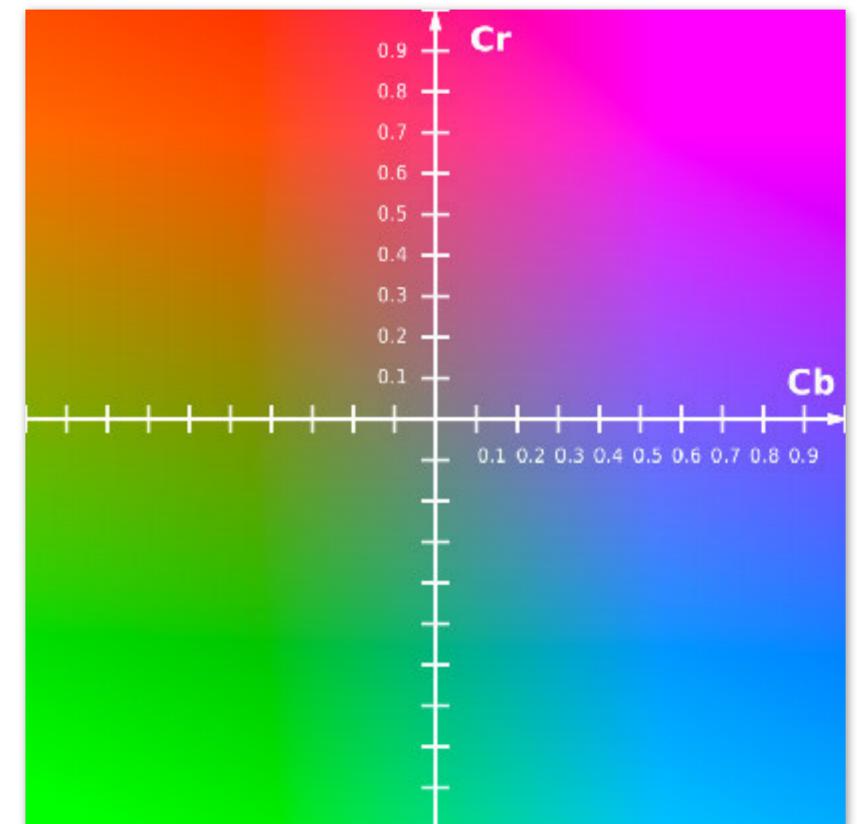
- Common for modern digital video
- $Y'$  = luma: perceived luminance (same as  $L^*$  in CIELAB)
- Cb = blue-yellow deviation from gray
- Cr = red-cyan deviation from gray



$Y'$



Cr





**Original picture of Kayvon**



**Contents of CbCr color channels downsampled by a factor of 20 in each dimension  
(400x reduction in number of samples)**



**Full resolution sampling of luma ( $Y'$ )**



**Reconstructed result  
(looks pretty good)**



**Original picture of Kayvon**

**By the way, how might we reduce this artifact?**



**Reconstructed result**

# Why use different color models? (cont.)

- **Convenience**
  - Is it easy for a user to choose the color they want?
- **Efficiency of encoding**
  - E.g., use more of numerical range for perceptually significant colors
  - Do color images *compress* well?
- **Gamut**
  - Which colors can be expressed using a given model?
  - Very different for print vs. display



RGB



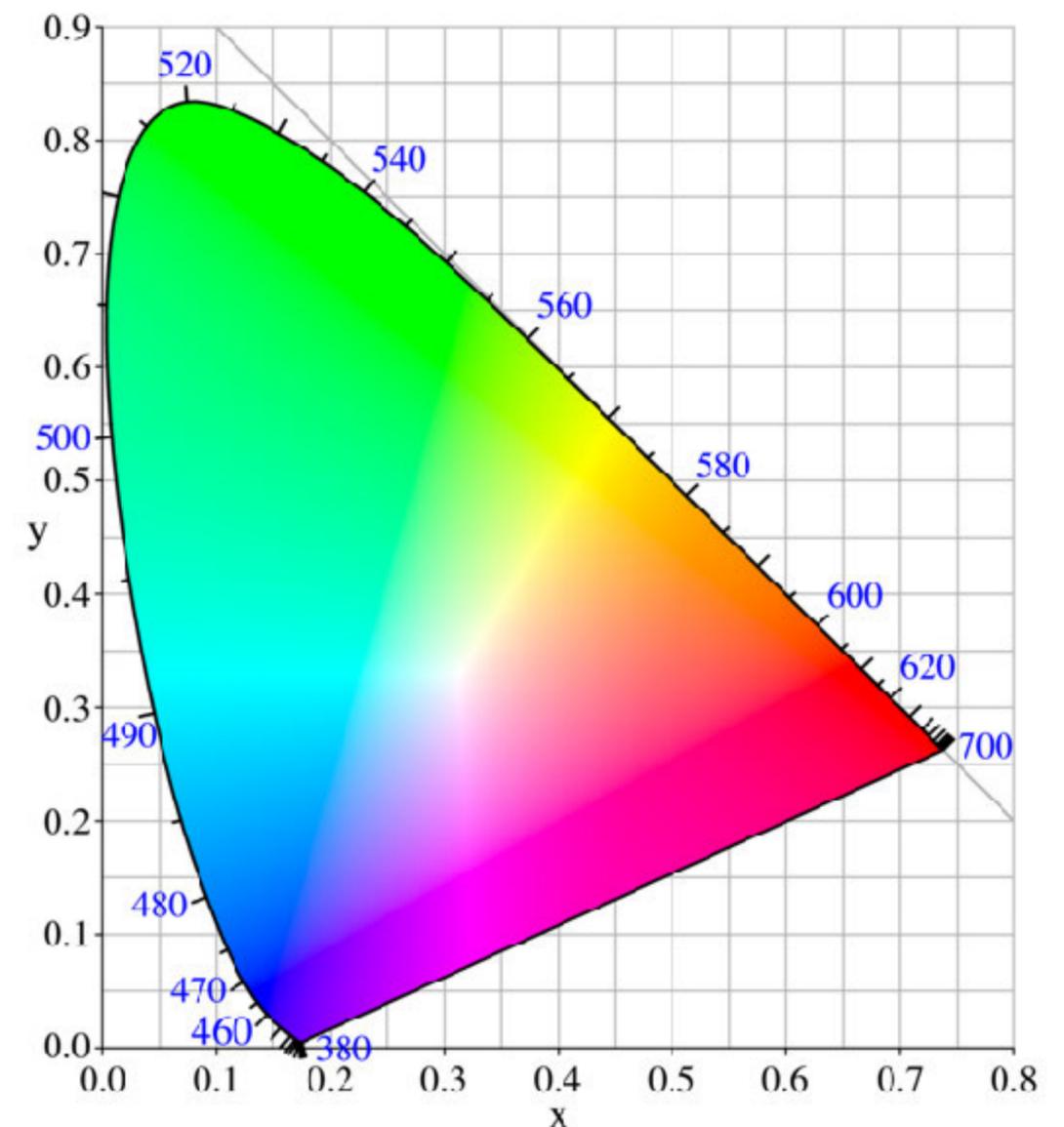
CMYK

**Which raises a very important question:**

**Which actual colors (i.e., *spectra*) do these values get mapped to?**

# CIE 1931\* Color Space

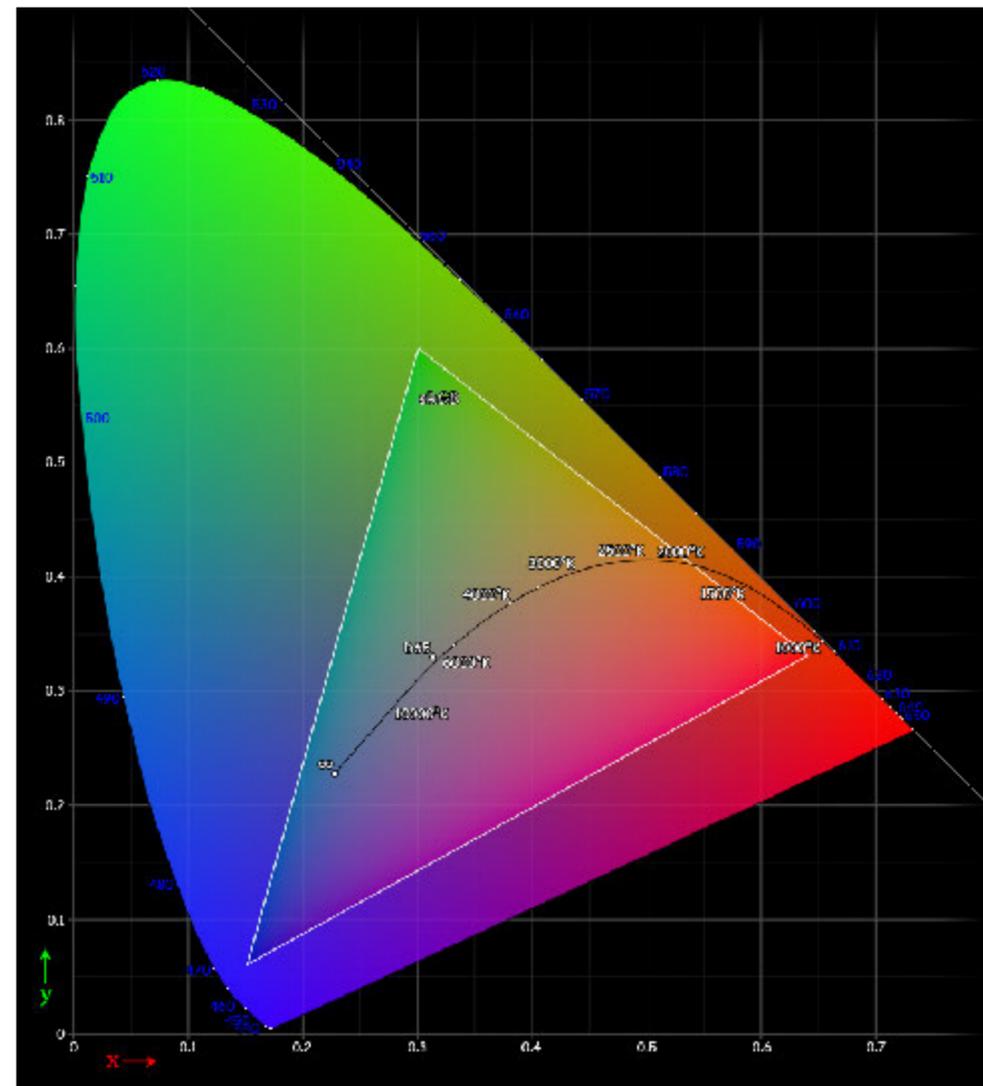
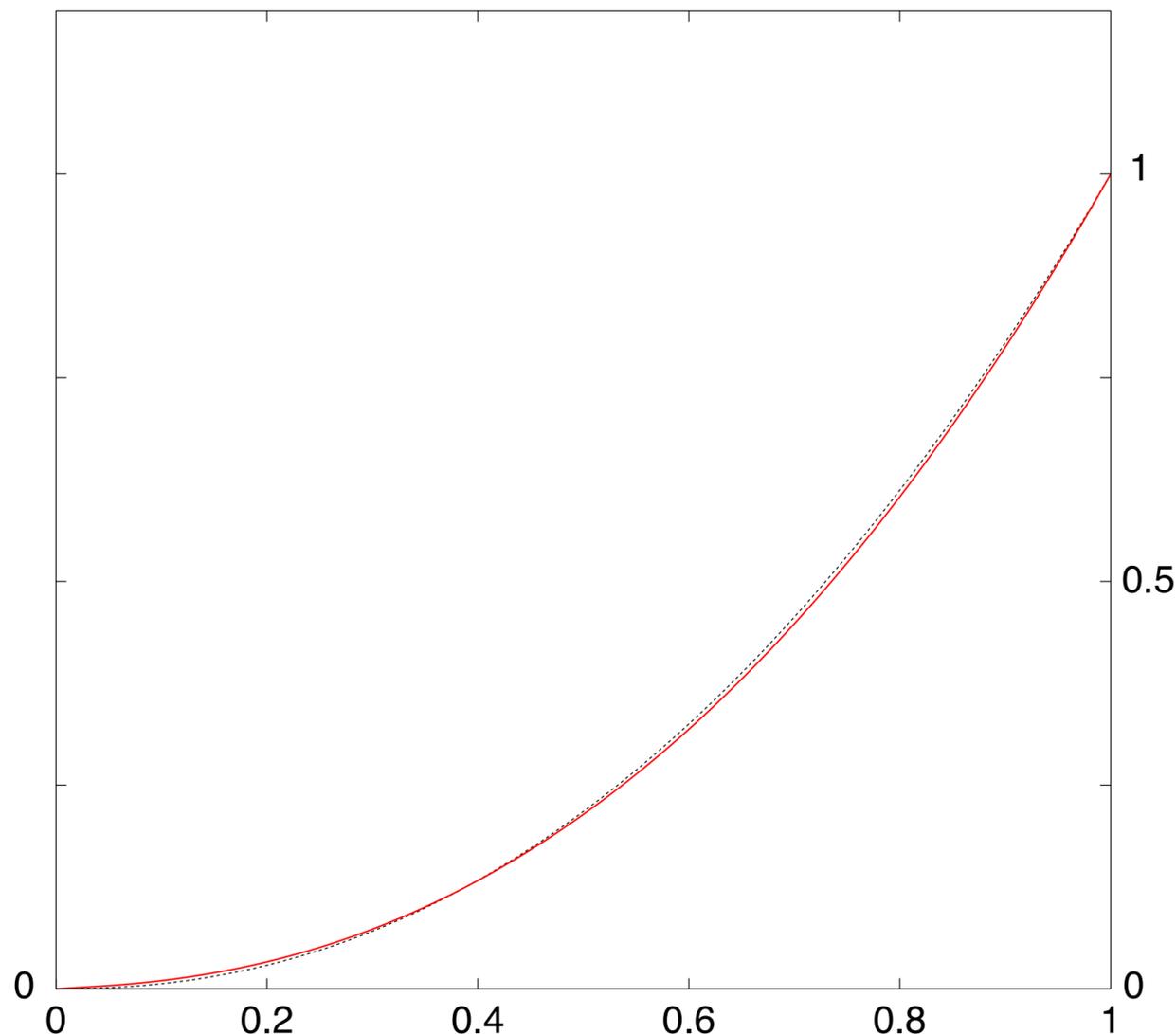
- Standard “reference” color space
- Encompasses all colors visible by “most” human observers
  - associated color *model* (XYZ) captures perceptual effects
  - e.g., perception of color (“chromaticity”) changes w/ brightness (“luminosity”)
  - different from specifying direct simulation of cones (SML)
  - ...*lots* more to say here!



\*CIE 1931 does not mean anything important: “created in 1931 by the Commission Internationale de l’Éclairage”

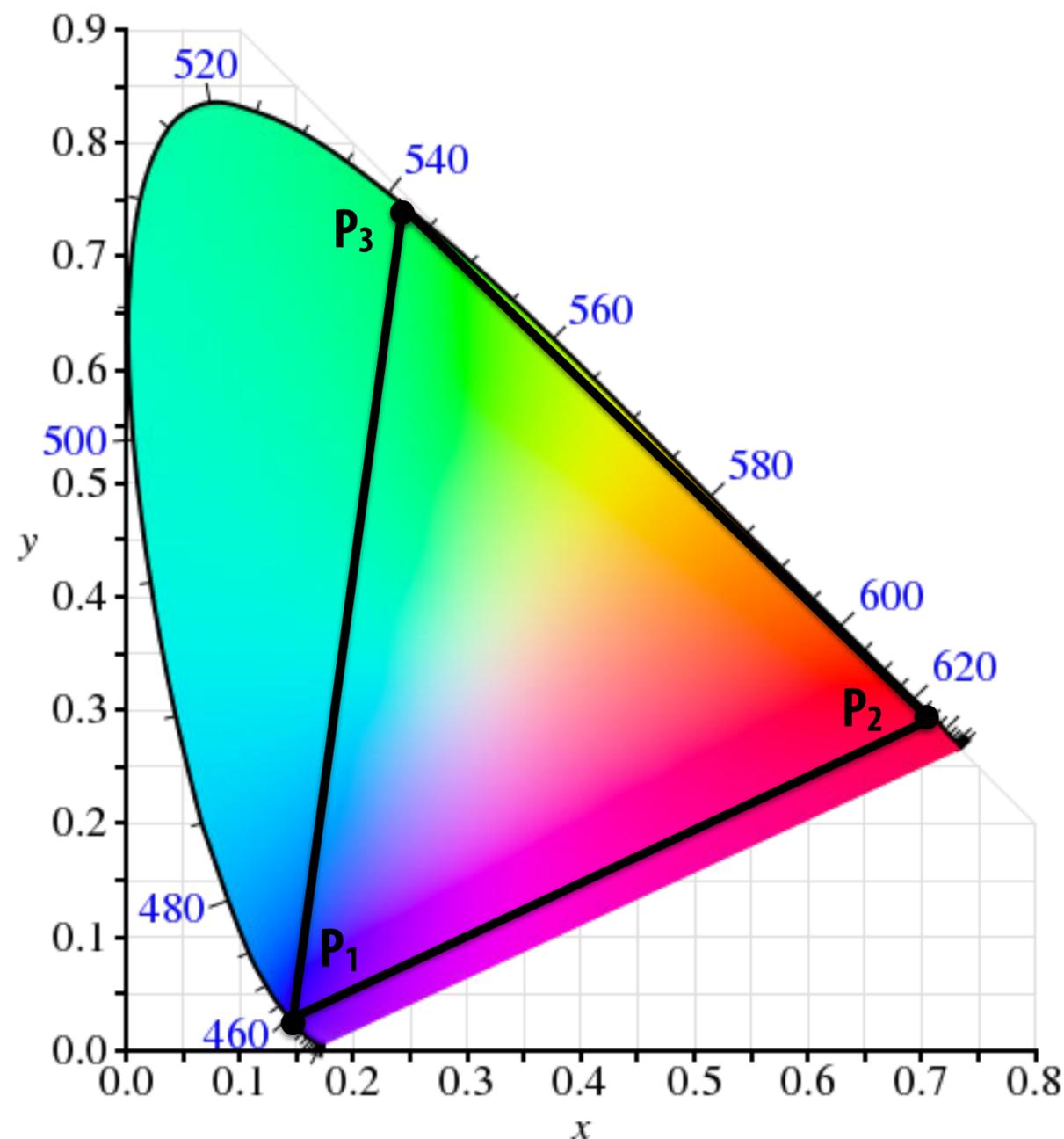
# sRGB Color Space

- CIE 1934 captured all possible human-visible colors
- sRGB (roughly) subset of colors available on displays, printers, ...
- Nonlinear relationship between stored RGB values & intensity
  - Makes better use of limited set of numerical values



# Chromaticity Diagrams

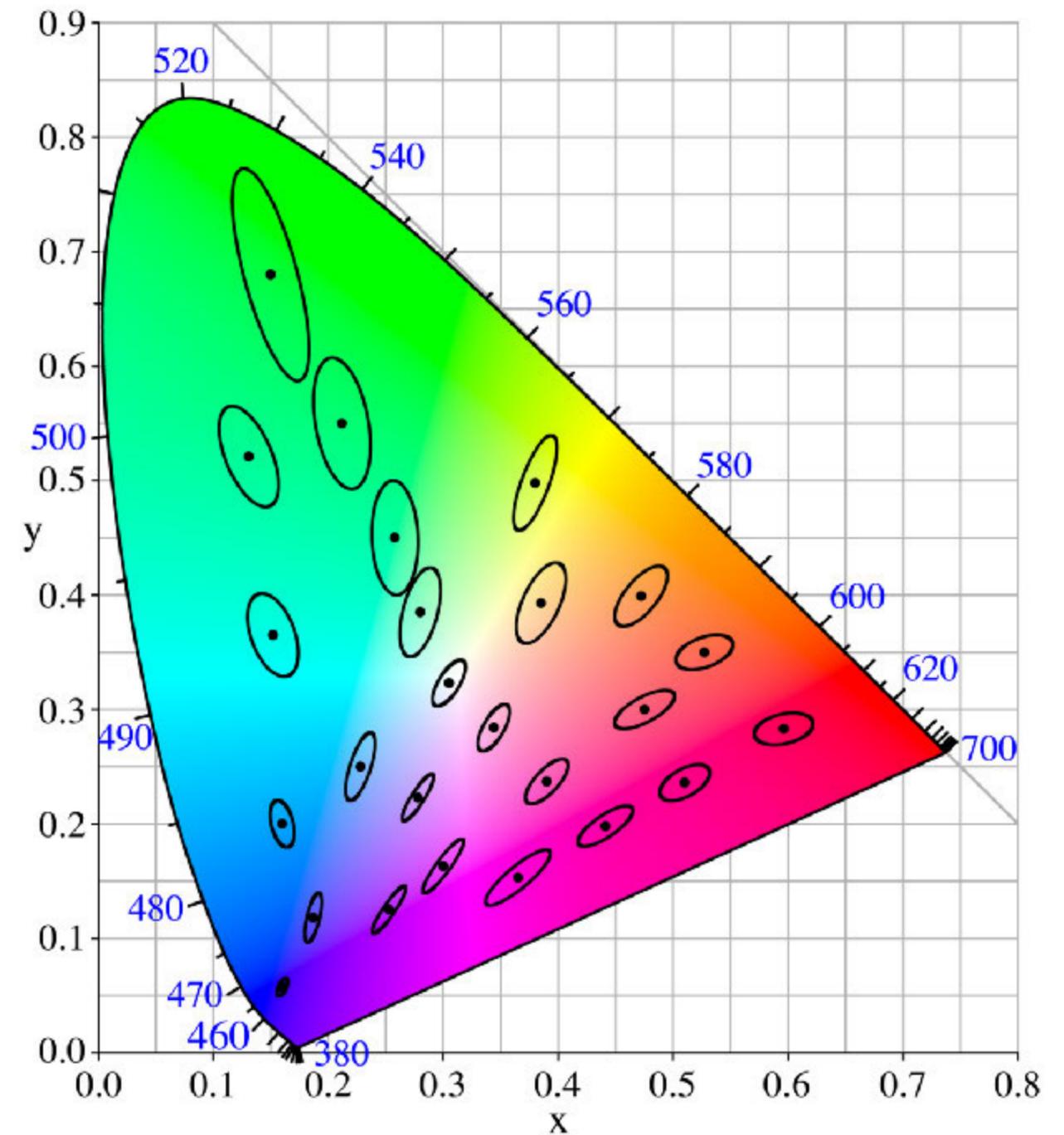
- Chromaticity is the intensity-independent component of a color
- Chromaticity diagram used to visualize extent of a color space



A display with primaries with chromacities  $P_1, P_2, P_3$  can create colors that are combinations of these primaries (colors that fall within the triangle)

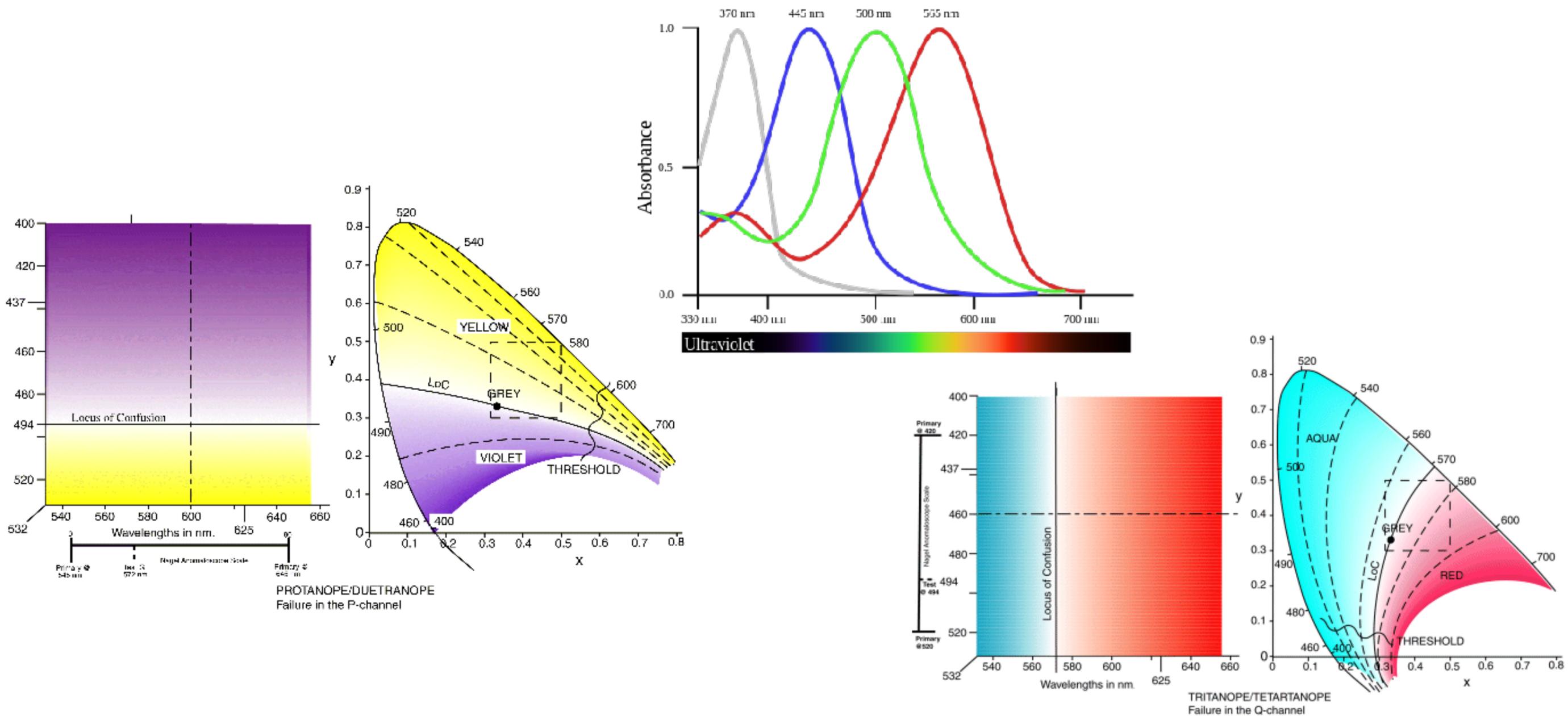
# Color Acuity (MacAdam Ellipse)

- In addition to *range* of colors visible, one might be interested in how *sensitive* people are to changes in color
- Each ellipse corresponds to a region of “just noticeable differences” of color (chromaticity)
- So, if you want to make two colors distinct, might try to avoid overlapping ellipses...



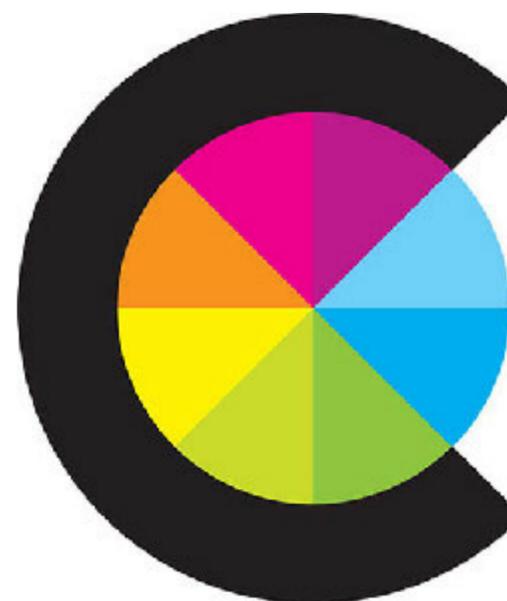
# Nonstandard Color Vision

- Morphological differences in eye can cause people (& animals) to see different ranges of color (e.g., more/fewer cone types)
- Alternative chromaticity diagrams help visualize color gamut, useful for designing, e.g., widely-accessible interfaces



# Color Conversion

- Given a color specified in one model/space (e.g., sRGB), try to find corresponding color in another model (e.g., CMYK)
- In a perfect world: want to match *output spectrum*
- Even matching *perception* of color would be terrific (metamers)
- In reality: may not always be possible!
  - Depends on the gamut of the output device
  - E.g., VR headset vs. inkjet printer
- Complicated task!
- Lots of standards & software
  - ICC Profiles
  - Adobe Color Management, ...



# Gamma correction

(non-linear correction for CRT display)

Old CRT display: 



1. Image contains value  $X$
2. CRT display converts digital signal to an electron beam voltage  $V(x)$  (linear relationship)
3. Electron beam voltage converted to light: (non-linear relationship)

$$Y \propto V^\gamma$$

Where:  $\gamma \approx 2.5$

So if pixels store  $Y$ , what will the display's output look like?

Fix: pixels sent to display must store:

$$Y^{1/2.5} = Y^{0.4}$$

(Doesn't apply to modern LCD displays, whose luminance output is linearly proportional to input; DOES still apply to other devices, like sensors, etc.)



Observed  
display output

Desired  
display output



# Human Perception—Accommodation Effect

# Next time...

- **A whole spectrum of things to know about light & color**
- **In the next few lectures we'll talk more about**
  - **radiometry**
  - **cameras**
  - **scattering**
  - **...**

